

$$3. y = x^{\frac{1}{3}}$$

$$y' = \frac{1}{3}x^{-\frac{2}{3}}$$

$$6. h(x) = \frac{2}{3}x^{\frac{1}{2}}$$

$$h'(x) = -\frac{1}{3}x^{-\frac{3}{2}}$$

$$9. f(x) = -x^2$$

$$f'(x) = -2x$$

$$12. y = t^3 + 2t^2 - 1$$

$$y' = 3t^2 + 4t$$

$$17. y = x^3 + \frac{4}{3}x^2 - 5x + 1$$

$$y' = 3x^2 + \frac{8}{3}x - 5$$

$$22. f(x) = \sqrt{x^3}$$

$$f'(x) = \frac{3}{2}x^{\frac{1}{2}}$$

$$24. y = \frac{x^{\frac{4}{3}}}{2}$$

$$y' = \frac{2}{3}x^{\frac{1}{3}}$$

$$37. y = x^{3/2}$$

$$y' = \frac{3}{2}x^{1/2}$$

$$\text{At the point } (1, 1), y' = \frac{3}{2}(1)^{1/2} = \frac{3}{2} = m.$$

$$38. y = x^{-1}$$

$$y' = x^{-2} = -\frac{1}{x^2}$$

$$\text{At the point } \left(\frac{3}{4}, \frac{4}{3}\right), y' = -\frac{1}{\left(\frac{3}{4}\right)^2} = -\frac{16}{9} = m.$$

$$52. f(x) = x^4 + \frac{1}{\sqrt{2}} - 5x^2$$

$$f'(x) = 4x^3 + 10x^{-3} = 4x^3 + \frac{10}{x^3}$$

$$55. f(x) = x^{\frac{5}{4}} + 2x$$

$$f'(x) = \frac{5}{4}x^{\frac{1}{4}} + 2$$

$$59. f(x) = \frac{3x^3 - x^2 + x + \sqrt{x}}{x} = 3x^2 - x + 1 + x^{\frac{1}{2}}$$

$$f'(x) = 6x - 1 - \frac{1}{2}x^{-\frac{3}{2}} = 6x - 1 - \frac{1}{2\sqrt{x^3}}$$

$$60. f(x) = \frac{2x^2 - 3x + 1}{x} = 2x - 3 + x^{-1}$$

$$f'(x) = 2 - x^{-2} = 2 - \frac{1}{x^2} = \frac{2x^2 - 1}{x^2}$$

73. (a) 2005:  $m \approx 119.2$ ; 2007:  $m \approx 161$
- (b) These results are close to the estimates in Exercise 13 in Section 2.1.
- (c) The slope of the graph at time  $t$  is the rate at which sales are increasing in millions of dollars per year.

77.  $C = 7.75x + 500$

$C' = 7.75$ , which equals the variable cost.

78.  $C = 150x + 7000$

$$P = R - C$$

$$P = 500x - (150x + 7000)$$

$$P = 350x - 7000$$

$P' = 350$ , which equals the profit on each dinner sold.