

Linear algebra exercise 03162017

1. (15 points) Let \mathbf{w} be a vector in \mathbf{R}^n . Let W be the set of vectors that are orthogonal to \mathbf{w} . Show that W is a subspace of \mathbf{R}^n .
2. (15 points) Find a basis for the subspace W of vectors that are orthogonal to $\mathbf{w} = (1, 3, 1)$. Give the dimension and a geometrical description of W .
3. (30 points) State and prove the Cauchy-Schwartz inequality
4. (15 points) State and prove triangle inequality
5. (15 points) State and prove pythagorean theorem