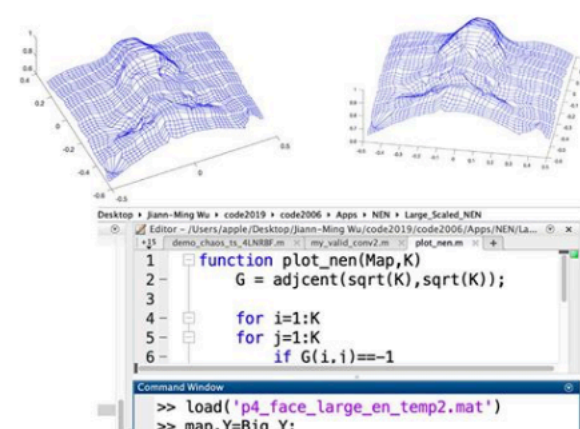


Matlab

Taylor expansion

$$f(a + \delta) \sim f(a) + \sum_{k=1}^K \frac{1}{k!} f^{(k)}(a) \delta^k$$

人工智慧基礎課程
備課點心



Exercise

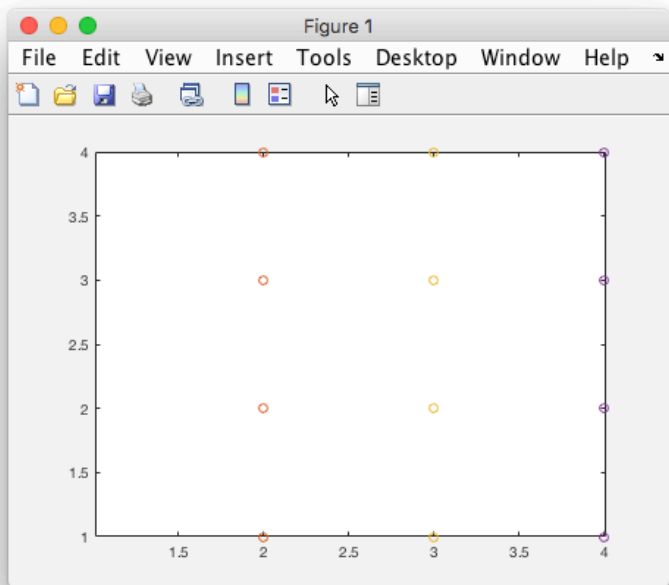
```
function demo_ex()
% step 1. Apply Matlab statement taylor to
% find Maclaurin series expansion of exp(-x^2)
% and set it to p

% step 2. Translate p to an inline px

% step 3. Set a = 1/2 and delta = 0.01
% and substitute a + delta to inline px
```

右圖中十六個點呈4x4方陣排列，矩陣X的元素代表相對應方陣點的橫坐標，Y矩陣的元素代表相對應方陣點的縱坐標。請完成下列程式，畫出方陣點

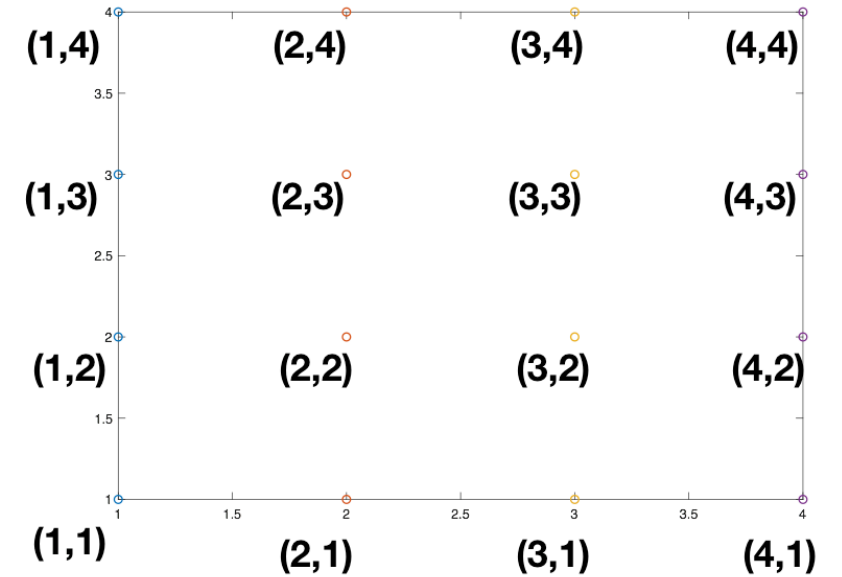
```
Command Window
n = 4;
a = linspace(1,n,n);
X =           ;
Y =           (X);
plot(X,Y,'o')
>>
>>
>>
>>
>>
>>
>>
>>
>>
fx >>
```



$$a = [1\ 2\ 3\ 4]$$

$$X = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \end{bmatrix}$$

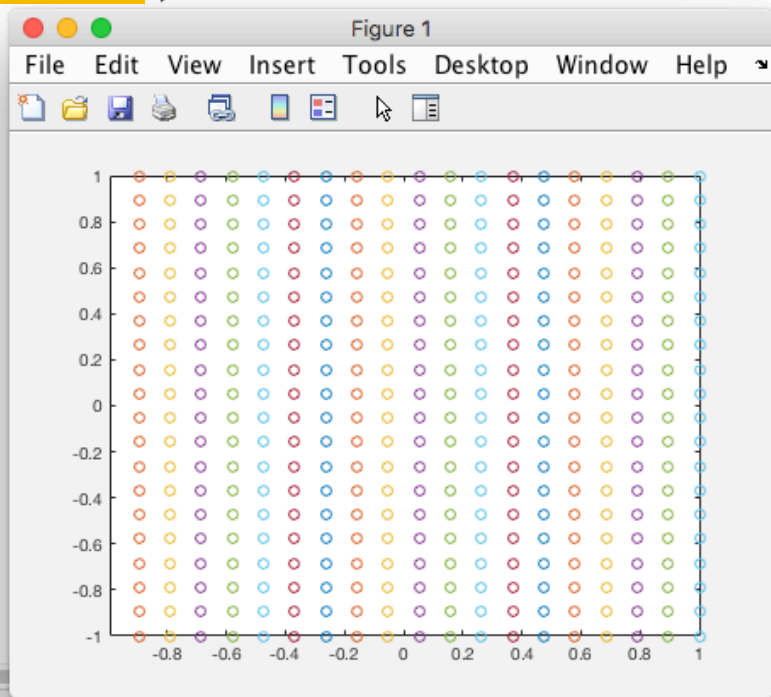
$$Y = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 2 & 2 & 2 & 2 \\ 3 & 3 & 3 & 3 \\ 4 & 4 & 4 & 4 \end{bmatrix}$$



在[-1, 1]x[-1, 1]的區域中繪製20x20的點矩陣

```
n = 20;  
a = _____;  
X = _____;  
Y = _____;  
plot(X,Y,'o')  
>>  
>>  
>>  
>>  
>>  
>>  
>>  
>>  
>>  
fx
```

本題答題

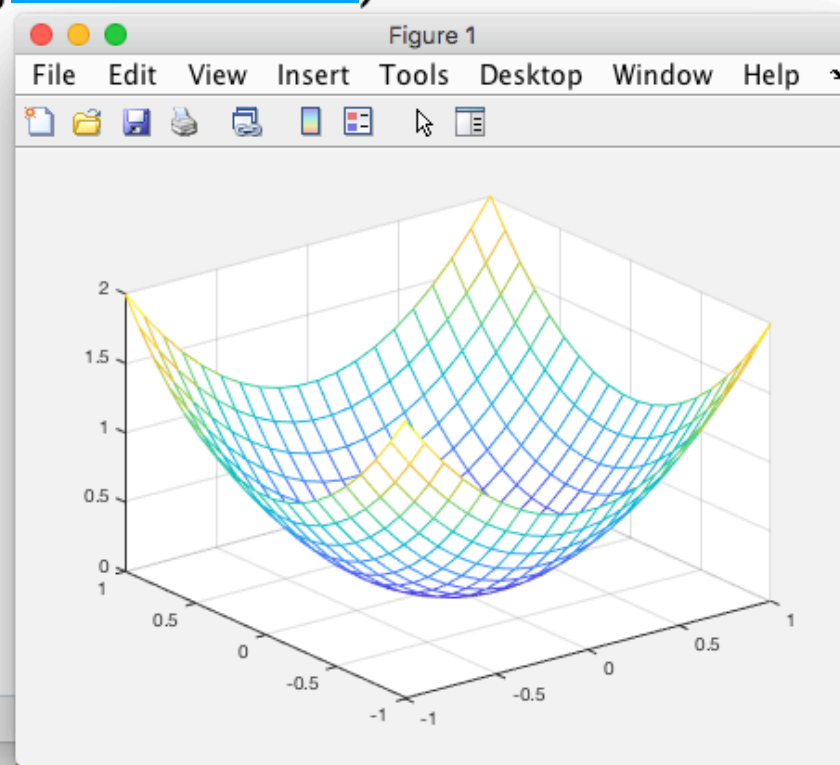


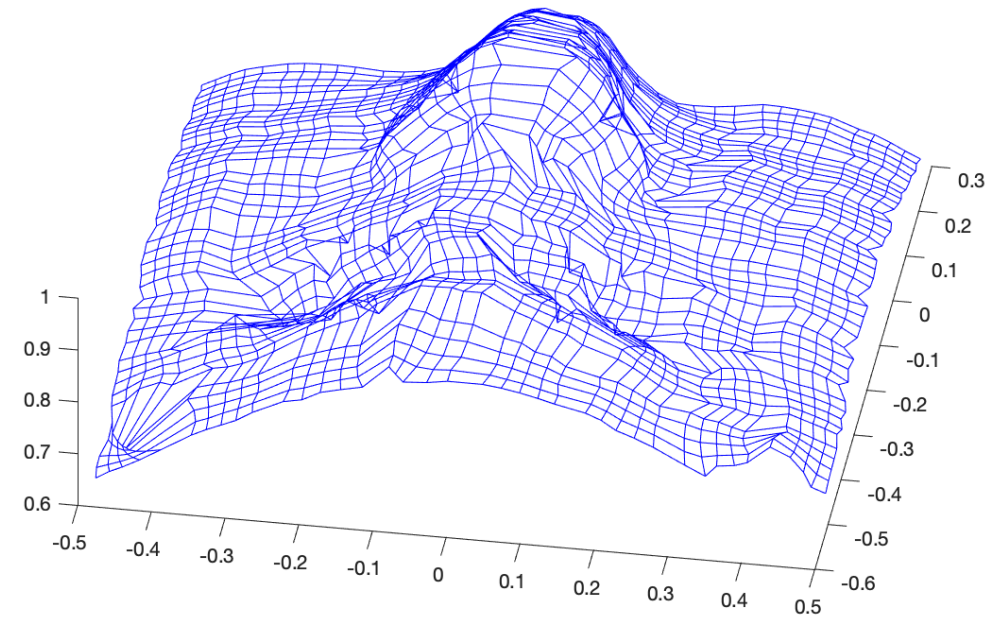
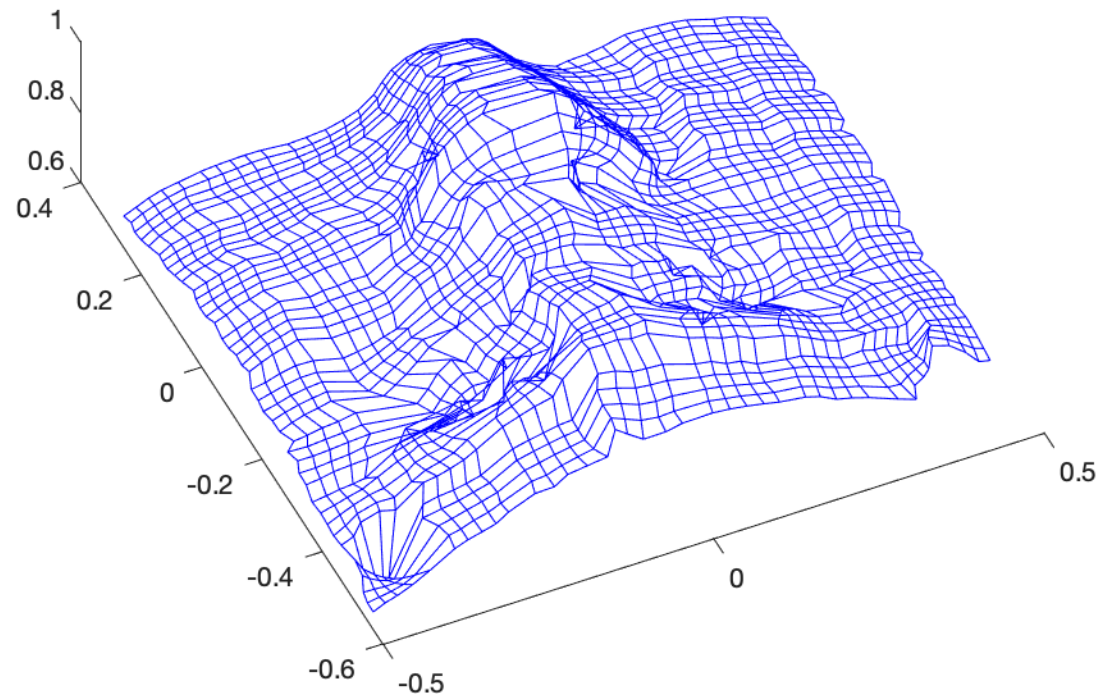
請完成mesh指令，繪製 $f(x, y) = x^2 + y^2$ 的立體圖

```
n = 20;  
a = _____;  
X = _____;  
Y = _____;  
mesh(a,a, _____)
```

fx >>

本題答題





Desktop ▸ Jiann-Ming Wu ▸ code2019 ▸ code2006 ▸ Apps ▸ NEN ▸ Large_Scaled_NEN

```

Editor - /Users/apple/Desktop/Jiann-Ming Wu/code2019/code2006/Apps/NEN/La...
demo_chaos_ts_4LNRBF.m  my_valid_conv2.m  plot_nen.m  +
1  function plot_nen(Map,K)
2  -      G = adjcent(sqrt(K),sqrt(K));
3
4  -      for i=1:K
5  -      -      for j=1:K
6  -      -      -      if G(i,i)==-1

```

```

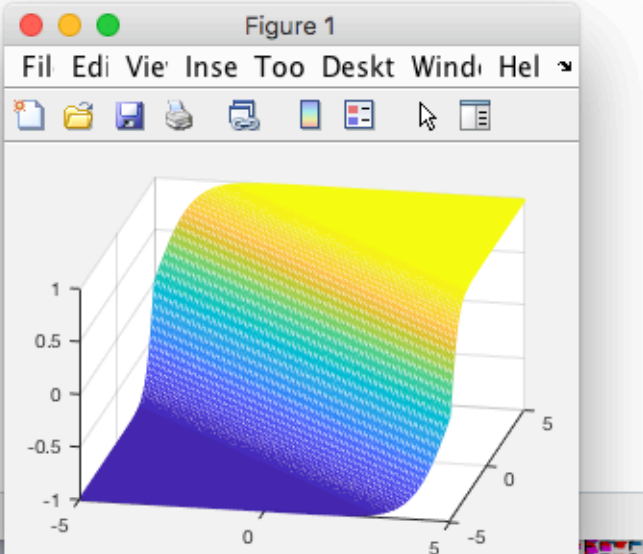
Command Window
>> load('p4_face_large_en_temp2.mat')
>> map.Y=Big_Y;
>> plot_nen(map,40*40)
>> plot_nen(map,40*40)

```


請完成mesh指令，繪製 $f(x, y) = \tanh(x + y)$ 的立體圖

```
n = 100;  
a = linspace(-5,5,n);  
X = _____;  
Y = _____;  
mesh(a,a, _____)  
>>  
>>  
>>  
>>  
>>  
>>  
fx >>  
Core36 demo.zip
```

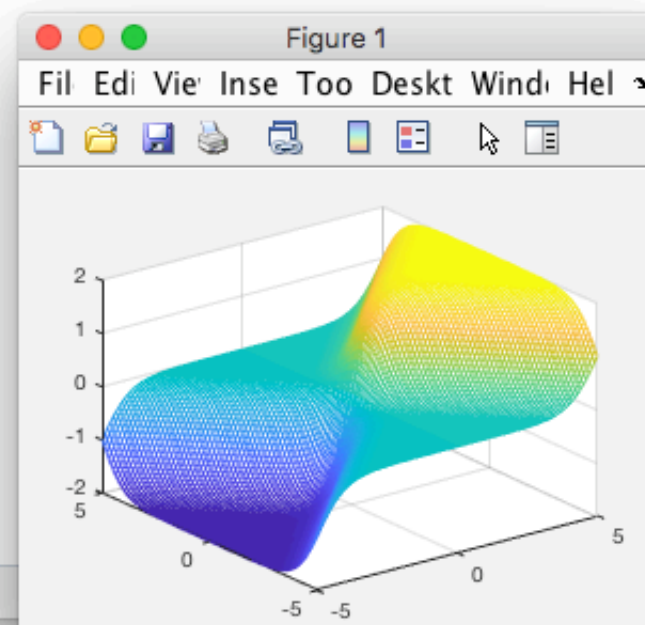
本題答題



請完成mesh指令，繪製 $f(x, y) = \tanh(x + y) + \tanh(x - y)$ 的立體圖

```
n = 100;  
a = linspace(-5,5,n);  
X = _____;  
Y = _____;  
mesh(a,a, _____)
```

```
>>  
>>  
>>  
>>  
>>  
>>  
>>  
fx >>
```



本題答題

Find the Maclaurin series expansions of the exponential, sine, and cosine functions up to the fifth order.

```
syms x
T1 = taylor(exp(x))
T2 = taylor(sin(x))
T3 = taylor(cos(x))
```

$$f(a + \delta) \sim f(a) + \sum_{k=1}^K \frac{1}{k!} f^{(k)}(a) \delta^k$$

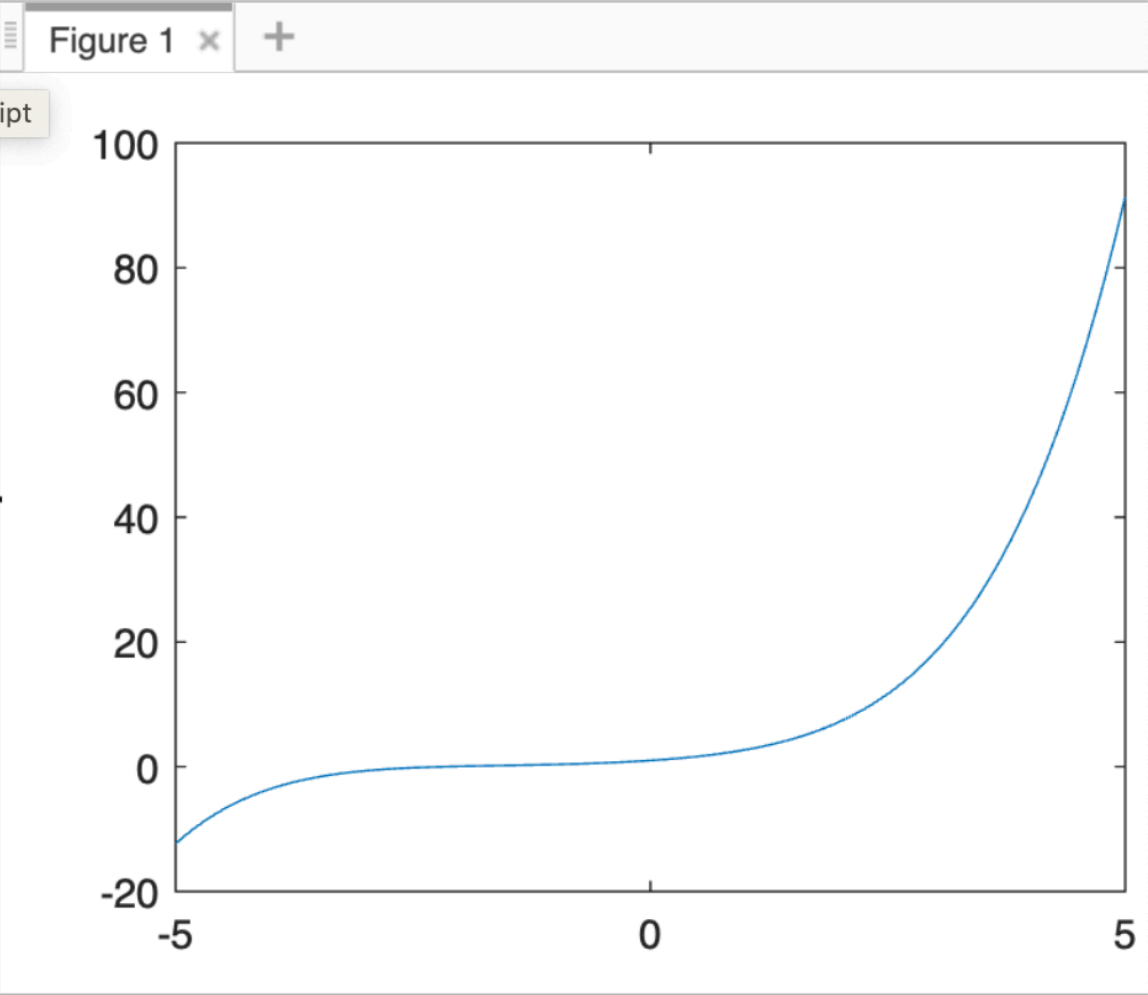
Exercise taylor_ex1

```
function taylor_ex1()  
% step 1. Apply Matlab statement taylor to  
%      find Maclaurin series expansion of exp(-x^2)  
%      and set it to p  
  
% step 2. Translate p to an inline px  
  
% step 3. Set a = 1/2 and delta = 0.01  
%      and substitute a + delta to inline px
```

Rich text editor toolbar with options: Bold, Italic, Monospaced, Hyperlink, Inline LaTeX, Bulleted List, Numbered List, Image, Preformatted Text, Code, Display LaTeX, Publish as HTML, Publish as PDF.

/ > MATLAB Drive >

```
1 function demo_Taylor_ex1_jmwu()  
2  
3     syms x;  
4     p = taylor(exp(x));  
5     px = inline(p);  
6     a = linspace(-5,5,100);  
7     plot(a,px(a))  
8  
9 end
```



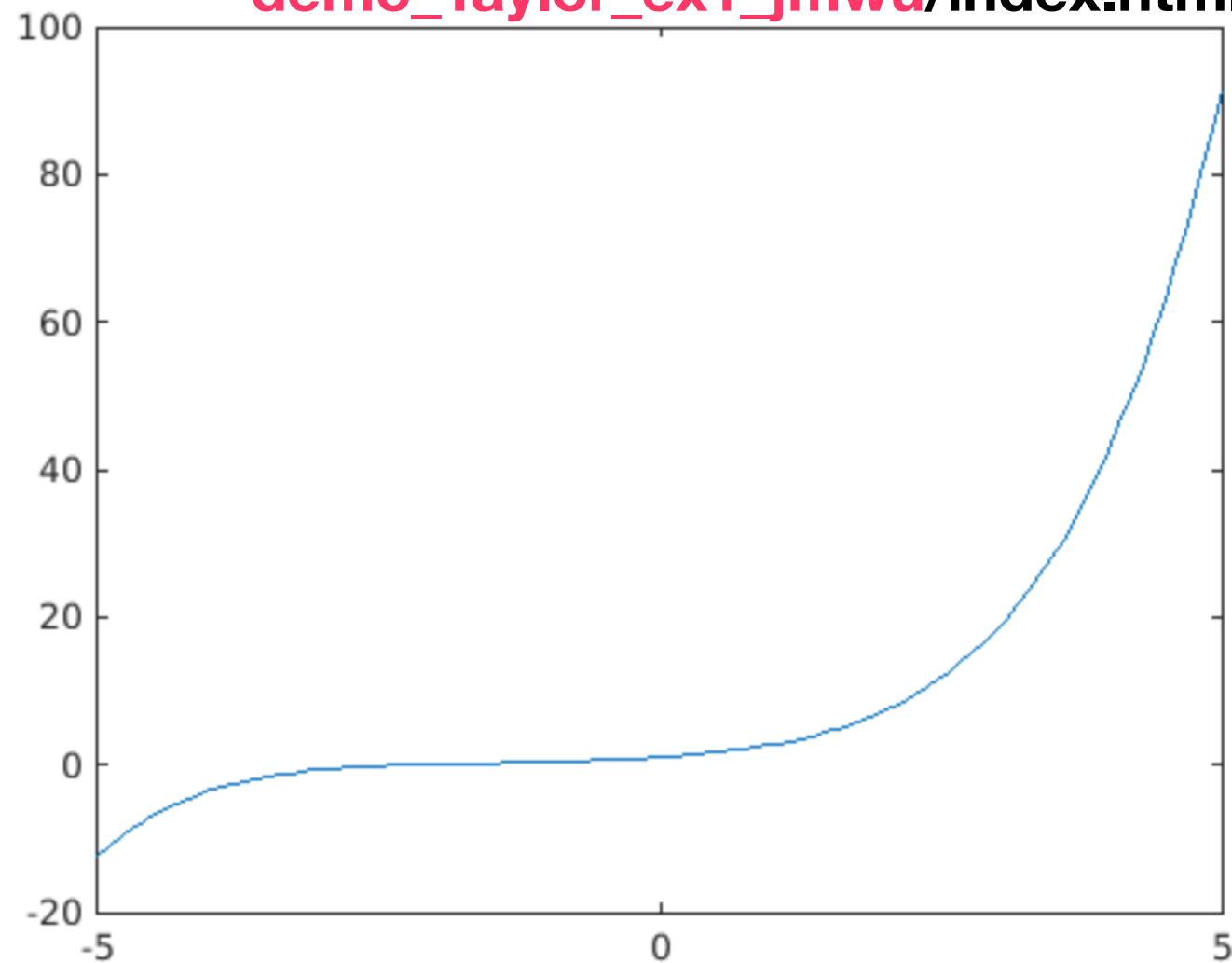
COMMAND WINDOW

New to MATLAB? See resources for [Getting Started](#).

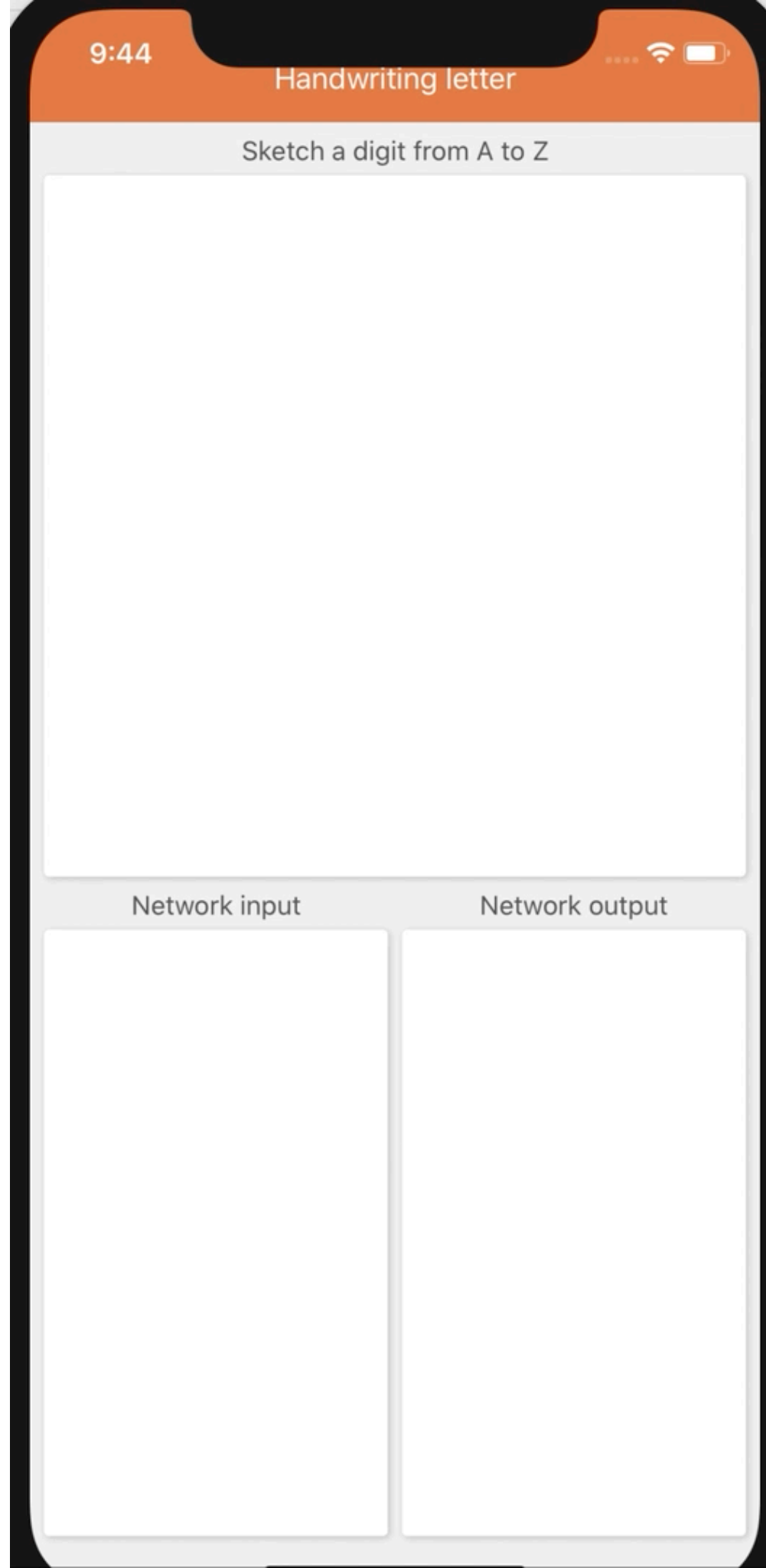


```
function demo_Taylor_ex1_jmwu()  
  
    syms x;  
    p = taylor(exp(x));  
    px = inline(p);  
    a = linspace(-5,5,100);  
    plot(a,px(a))  
  
end
```

https://matlab.mathworks.com/users/jmwu@mail.ndhu.edu.tw/Published/demo_Taylor_ex1_jmwu/index.html



LetterCore36



9:50

Handwriting letter



Sketch a digit from A to Z

Network input

Network output

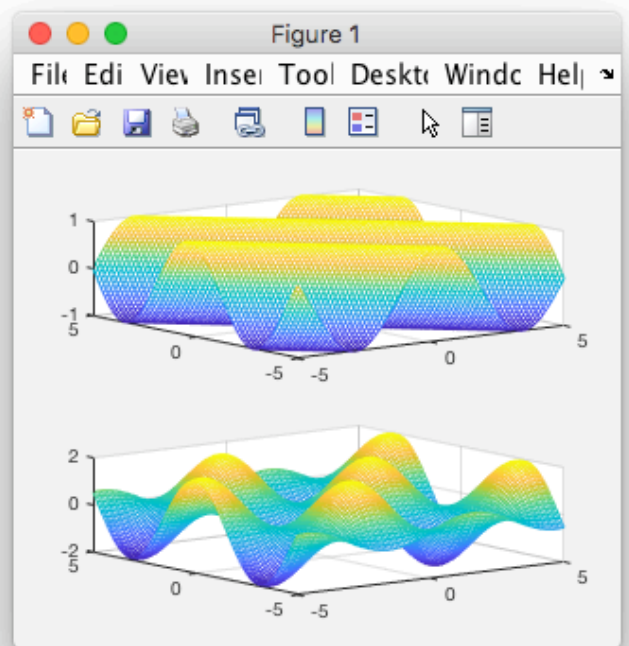
LetterCore38

請完成mesh指令，繪製 $f(x, y) = \sin(x + y) + \sin(x - y)$ 的立體圖

```
n = 100;  
a = linspace(-5,5,n);  
X = _____;  
Y = _____;  
_____  
mesh(a,a,sin(X+Y))  
subplot(2,1,2)  
mesh(a,a,_____)
```

```
>>  
>>  
>>  
>>  
>>  
>>  
>>  
>>  
>>  
fx >>
```

本題答題



請完成下列程式，印出 $x^3 - 2x + 1$ 的一階導數、二階導數及三階導數

```
Command Window
x = ('x');
s = diff(x^3-2*x+1)
for i = 2:3
    s = (s)
end

s =

3*x^2 - 2

s =

6*x

s =

fx 6
```

請將代表 $x^3 - 2x + 1$

的一階導數、二階導數與三階導數的字串分別儲存於cell， $s\{1\}$ 、 $s\{2\}$ 與 $s\{3\}$

```
x = sym('x');  
s{1} = diff(x^3-2*x+1);  
display(s{1})  
for i = 2:3  
    s{i} =                     ;  
    display(s{i})  
end
```

ans =

$3*x^2 - 2$

ans =

$6*x$

ans =

6

請將代表 $x^3 - 2x + 1$

的一階導數、二階導數與三階導數的inline函數分別儲存於cell， f{1}、f{2}與f{3}

```
>>  
x = sym('x');  
s{1} = diff(x.^3-2*x+1);  
for i = 2:3  
    s{i} =           ;  
end  
for i = 1:3  
    f{i} =           ;  
    display(f{i})  
end
```

=

```
Inline function:  
(x) = x.^2.*3.0-2.0
```

=

```
Inline function:  
(x) = x.*6.0
```

=

```
Inline function:  
(x) = 6.0
```

Save Section Section with Title **B** Bold **I** Italic **M** Monospaced Hyperlink Inline LaTeX Bulleted List Numbered List Image Preformatted Text Code Display LaTeX Publish as HTML Publish as PDF

MATLAB Drive > Published >

CURRENT FOLDER

- sinch_plot_01.png
- sinch_plot.png
- sinch_plot.html
- demo_hagan_01.png
- demo_hagan.png
- demo_hagan.html
- third_derivatives

```
1 - syms x;  
2 - s{1} = diff(x.^3-2*x+1);  
3 - for i = 2:3  
4 -     s{i} = diff(s{i-1});  
5 - end  
6 - for i = 1:3  
7 -     f{i} = inline(s{i});  
8 -     display(f{i});  
9 - end
```

Press to publish

WORKSPACE

NAME	VALUE	SIZE	CLASS
ans	'/MATLAB ...	1x52	char
f	1x3 cell	1x3	cell
i	3	1x1	double
s	1x3 cell	1x3	cell
x	1x1 sym	1x1	sym

COMMAND WINDOW

New to MATLAB? See resources for Getting Started.

>>

Directory

Mail to cite to teaching assistant

https://
matlab.mathworks.com/users/
jmwu@mail.ndhu.edu.tw/
Published/
third_derivatives/
index.html

Your matlab user id

Published directory



```
syms x;  
s{1} = diff(x.^3-2*x+1);  
for i = 2:3  
    s{i} = diff(s{i-1});  
end  
for i = 1:3  
    f{i} = inline(s{i});  
    display(f{i});  
end
```

=

Inline function:
(x) = x.^2.*3.0-2.0

=

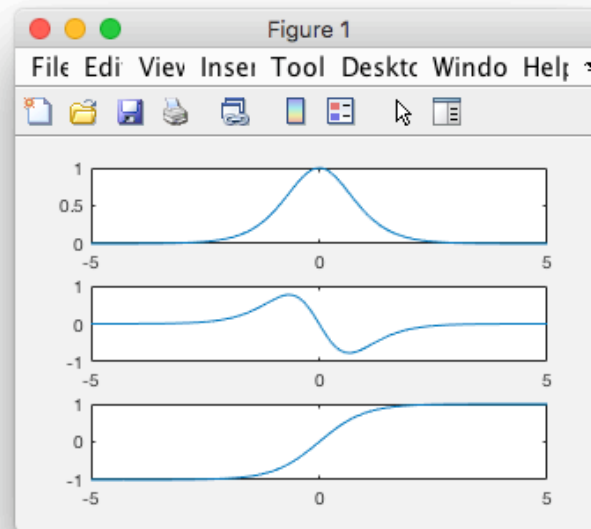
Inline function:
(x) = x.*6.0

=

Inline function:
(x) = 6.0

請以plot指令繪製f{i}所代表的inline函數，plot的兩個輸入參數分別為向量a，以及將向量a代入函數f{i}的結果

```
>> x = sym('x');  
s{1} = diff(tanh(x));  
for i = 2:3  
    s{i} =                     ;  
end  
a = linspace(-5,5);  
for i = 1:2  
    f{i} =                     ;  
    subplot(3, 1, i)  
                          
end  
subplot(3,1,3)  
plot(a, tanh(a))
```



本題求 $\tanh(a+da)$ 的泰勒展開，展開的項數為三，請將第一項的內容儲存在變數`app`，並在迴圈中將`da`的`k`次方項加入變數`app`中

```

K = 2; a = pi/4; da = 10^-2;
x = sym('x');
s{1} = diff(tanh(x));
for i = 2: K
    s{i} = diff(s{i-1});
end
fprintf('tanh(a+da) = %15.14f\n',tanh(a+da));
app =                     ;
for k = 1 : K
    f{k} = inline(s{k});
    app = app +                                                         ;
end
fprintf('app           = %15.14f\n', app);

tanh(a+da) = 0.66145622234088
app         = 0.66145616633167
  
```

$$f(a + \delta) \sim f(a) + f'(a)\delta + \frac{1}{2!}f''(a)\delta^2$$

本題求 $\tanh(a+da)$ 的泰勒展開，展開的項數為五，請將第一項的內容儲存在變數`app`，並在迴圈中將`da`的`k`次方項加入變數`app`中

```
K = 5; a = pi/4; da = 10^-2;
x = sym('x');
s{1} = diff(tanh(x));
for i = 2: K
    s{i} = diff(s{i-1});
end
fprintf('tanh(a+da) = %15.14f\n',tanh(a+da));
app = 0;
for k = 1 : K
    f{k} = inline(s{k});
    app = app + f{k}(a+da)*da^k;
end
fprintf('app = %15.14f\n', app);
tanh(a+da) = 0.66145622234088
app = 0.66145622234724
```

本題求 $\tanh(a+da)$ 的泰勒展開，展開的項數為七，請將第一項的內容儲存在變數`app`，並在迴圈中將`da`的`k`次方項加入變數`app`中

```
K = 7; a = pi/4; da = 10^-2;
x = sym('x');
s{1} = diff(tanh(x));
for i = 2:K
    s{i} = diff(s{i-1});
end
fprintf('tanh(a+da) = %15.14f\n',tanh(a+da));
app = 0;
for k = 1:K
    f{k} = inline(s{k});
    app = app + f{k}(a+da)*da^k;
end
fprintf('app = %15.14f\n', app);
tanh(a+da) = 0.66145622234088
app = 0.66145622234088
```

Exercise taylor_ex2

$$f(x) = \exp(-x^2)$$

$$f(a + \delta) \sim f(a) + \sum_{k=1}^K \frac{1}{k!} f^{(k)}(a) \delta^k$$

$$a = \frac{1}{2}, \quad \delta = 0.01$$

$$f(a + \delta) = ?$$

1. **Revise the Matlab script at page 20 to find Taylor expansions of e^{-x^2} with $K = 6$**
2. **Set $a = 1/2$ and $\delta = 0.01$
Substitute $a + \delta$ to the Taylor expansions**