

Deep Learning and Labeled Patterns

表格 1

```
>> A= reshape(1:9,3,3)
```

```
A =
```

```
1     4     7
```

```
2     5     8
```

```
3     6     9
```

```
>> B = reshape(1:16,4,4)
```

```
B =
```

```
1     5     9    13
```

```
2     6    10    14
```

```
3     7    11    15
```

```
4     8    12    16
```

```
>> conv2(B,A,'valid')
```

```
ans =
```

```
192  372
```

```
237  417
```

```
>> AA=A([3 2 1],:)
```

```
AA =
```

```
3 6 9  
2 5 8  
1 4 7
```

```
>> sum(sum(B(1:3,1:3).*BB))
```

```
ans =  
192
```

```
>> sum(sum(B(1:3,2:4).*BB))
```

```
ans =  
372
```

```
>> BB = AA(:,[3 2 1]);
```

```
>> BB
```

```
BB =
```

```
9 6 3  
8 5 2  
7 4 1
```

```
>> sum(sum(B(2:4,1:3).*BB))
```

```
ans =  
237
```

```
>> sum(sum(B(2:4,2:4).*BB))
```

```
ans =  
417
```

```
>>
```

Current Folder

- flip_all.m
- my_valid_conv2_matlab.m
- my_valid_conv2.m

```
1 function M = flip_all(K)
```

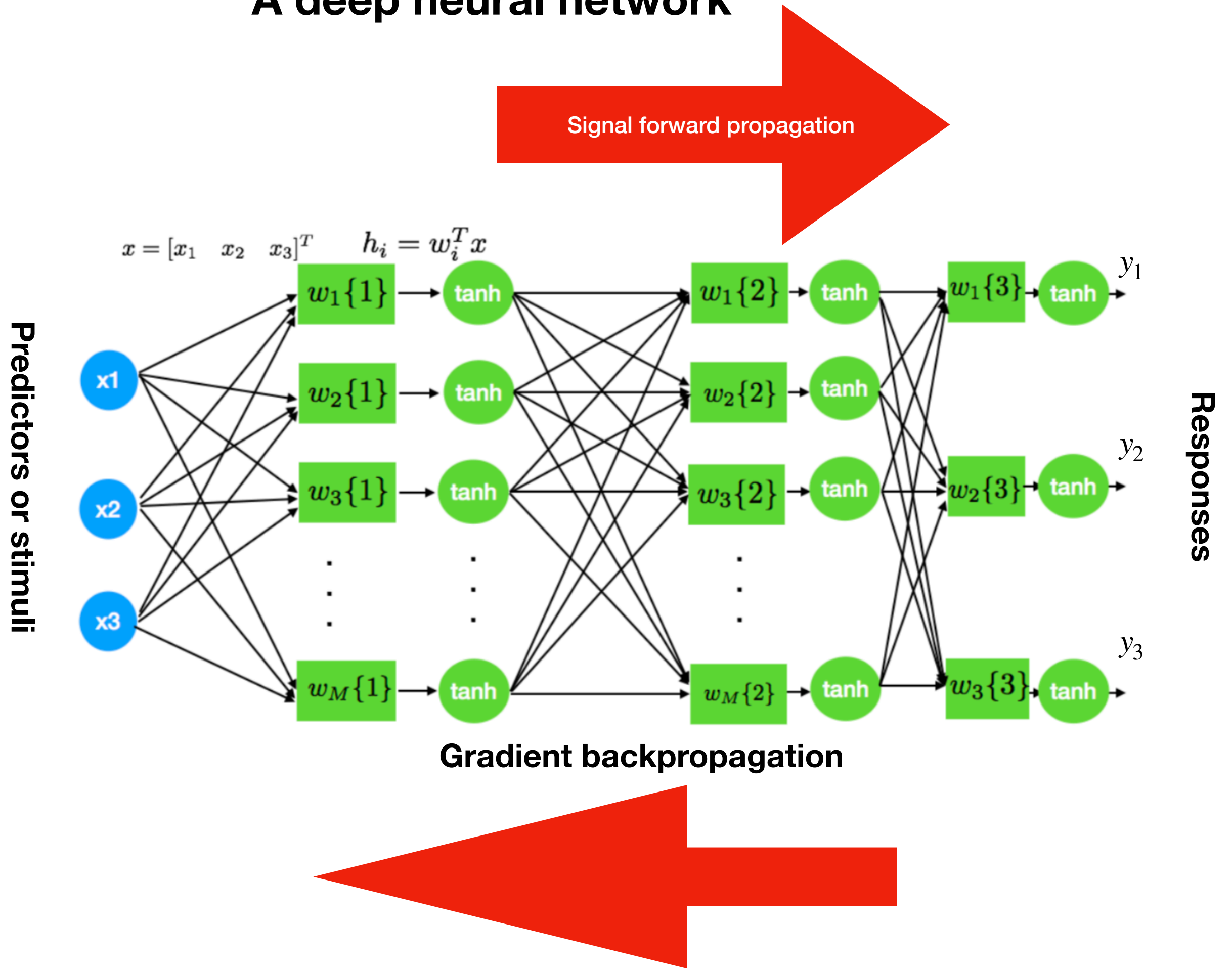
```
>> A = reshape(1:1:9,3,3);  
>> B = reshape(1:16,4,4);  
>> my_valid_conv2_matlab(B,A)  
  
ans =  
  
    192    372  
    237    417  
  
>> conv2(B,A,'valid')  
  
ans =  
  
    192    372  
    237    417  
  
fx >> |
```

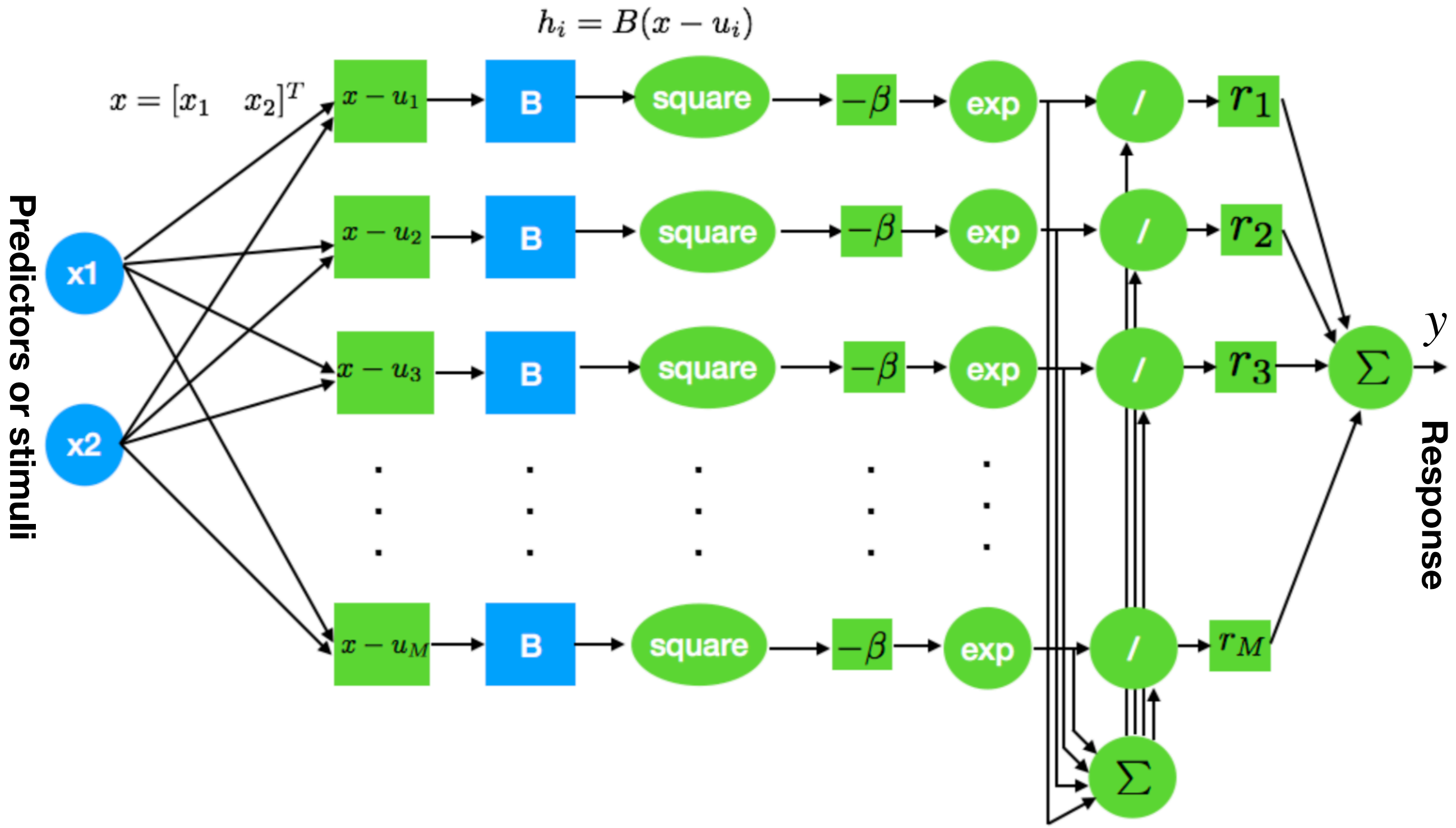
my_valid_conv2_matlab and conv2 produce the same result

Exercise I

Try to write a Matlab function that is equivalent to `conv2` for valid convolution.

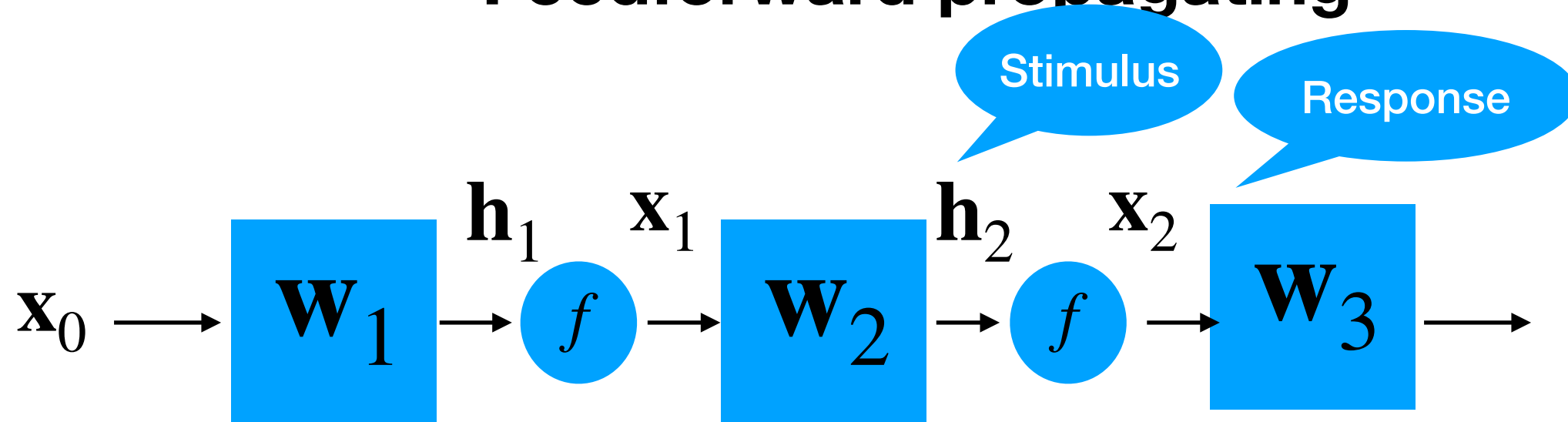
A deep neural network





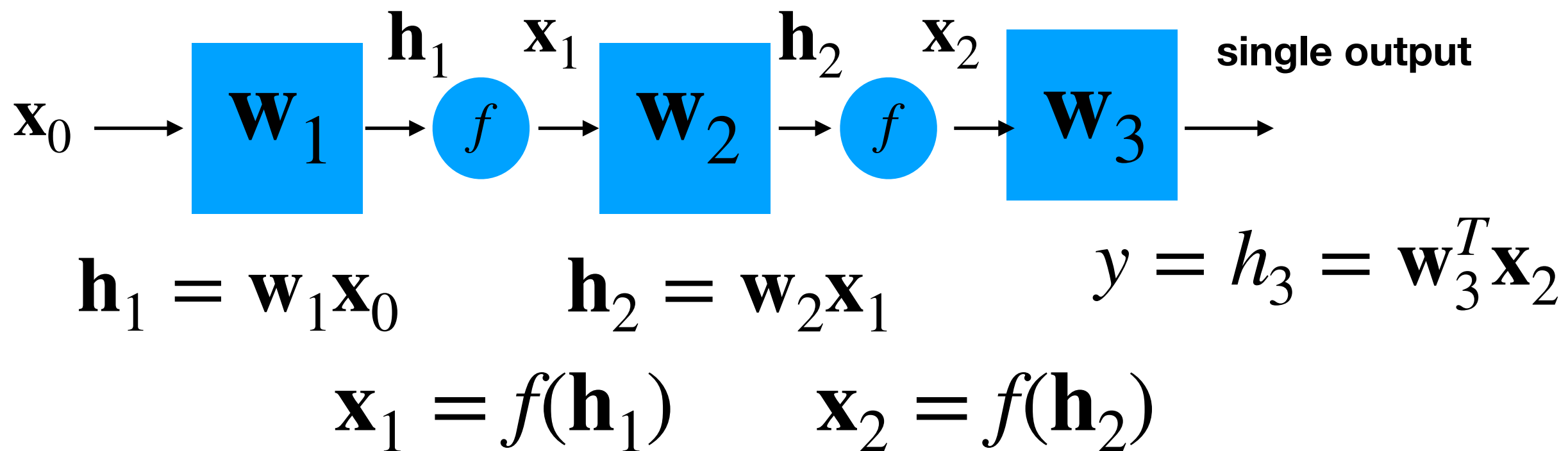
A Deep Neural Network with two hidden layers

Feedforward propagating



$$\mathbf{h}_1 = \mathbf{w}_1 \mathbf{x}_0 \quad \mathbf{h}_2 = \mathbf{w}_2 \mathbf{x}_1 \quad y = h_3 = \mathbf{w}_3^T \mathbf{x}_2$$
$$\mathbf{x}_1 = f(\mathbf{h}_1) \quad \mathbf{x}_2 = f(\mathbf{h}_2)$$

Gradients back-propagation



$\mathbf{x}_1(i) \quad \mathbf{w}_2(i, j) \quad \mathbf{h}_2(j)$

$\mathbf{h}_2(j) = \sum_k \mathbf{x}_1(k) w_2(k, j)$

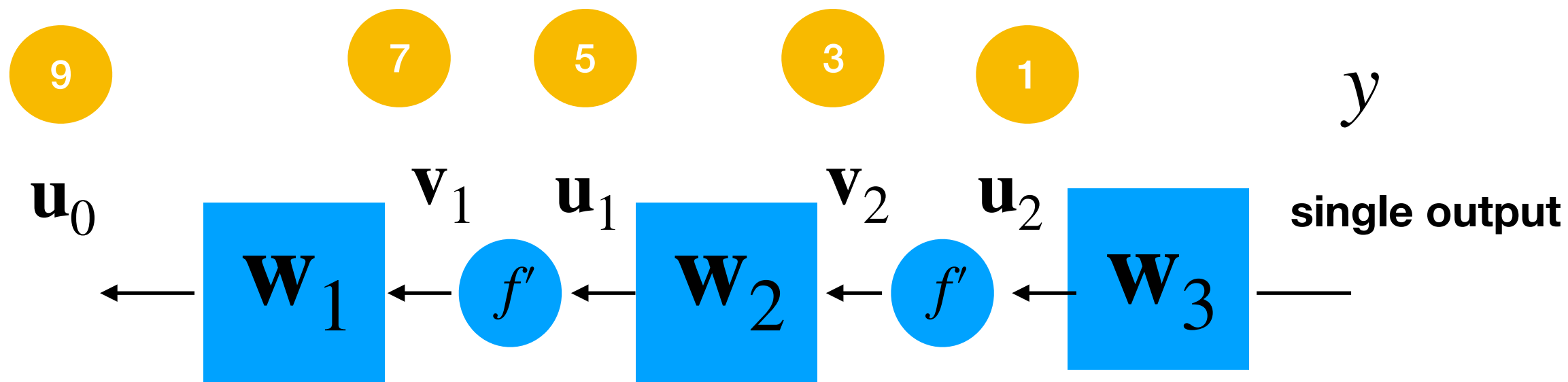
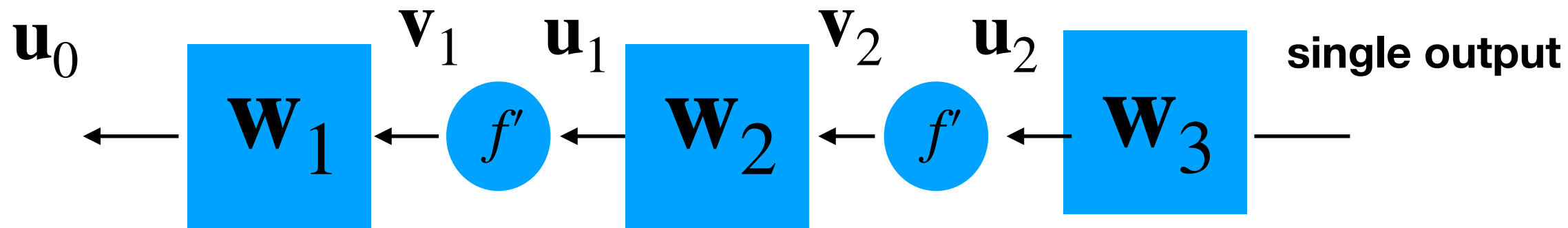
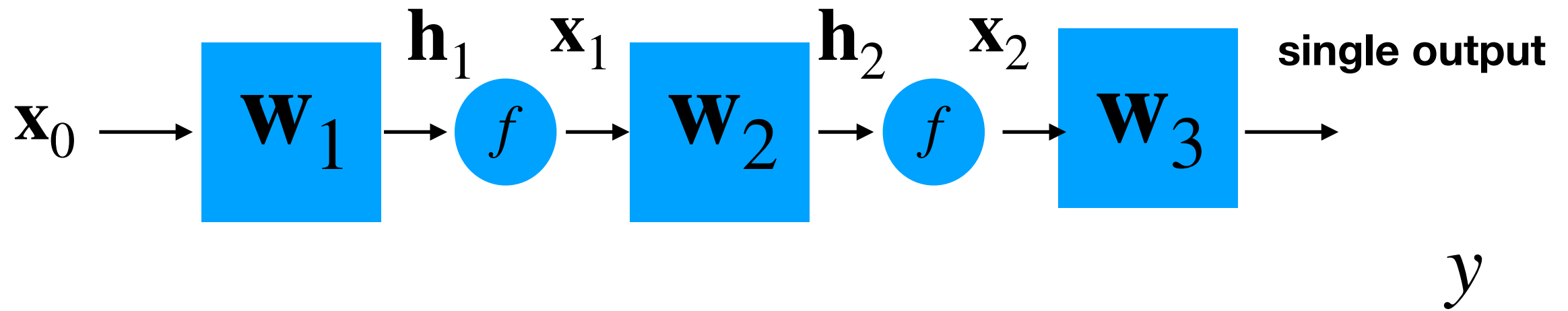


Diagram illustrating the calculation of the hidden layer output $\mathbf{h}_2(j)$ based on the input $\mathbf{x}_1(i)$ and the weight $w_2(i, j)$:

$$\mathbf{h}_2(j) = \sum_k \mathbf{x}(k) w_2(k, j)$$



Exercise II.A

Diagram illustrating the relationship between $\mathbf{x}_1(i)$ and $\mathbf{h}_2(j)$ via the weight $w_2(i, j)$.

$$\mathbf{h}_2(j) = \sum_k \mathbf{x}_1(k) w_2(k, j)$$

Let $v_2(j) = \frac{dy}{d\mathbf{h}_2(j)}$. $\frac{dy}{dw_2(i, j)} = ?$

Exercise II.B

$$\text{Let } \mathbf{v}_2(j) = \frac{dy}{d\mathbf{h}_2(j)}. \quad \frac{dy}{d\mathbf{w}_2(i,j)} = ?$$

Let $e = (t - y)^2$, where t denotes the desired target

$$\frac{de}{d\mathbf{w}_2(i,j)} = ?$$

Exercise II.C Show convergence of e for gradient descent learning.

Gradient descent learning

$$\Delta \mathbf{w}_2(i, j) = -\eta \frac{de}{d\mathbf{w}_2(i, j)}$$

where η is a small positive value

Multilayer Potts Perceptrons With Levenberg–Marquardt Learning

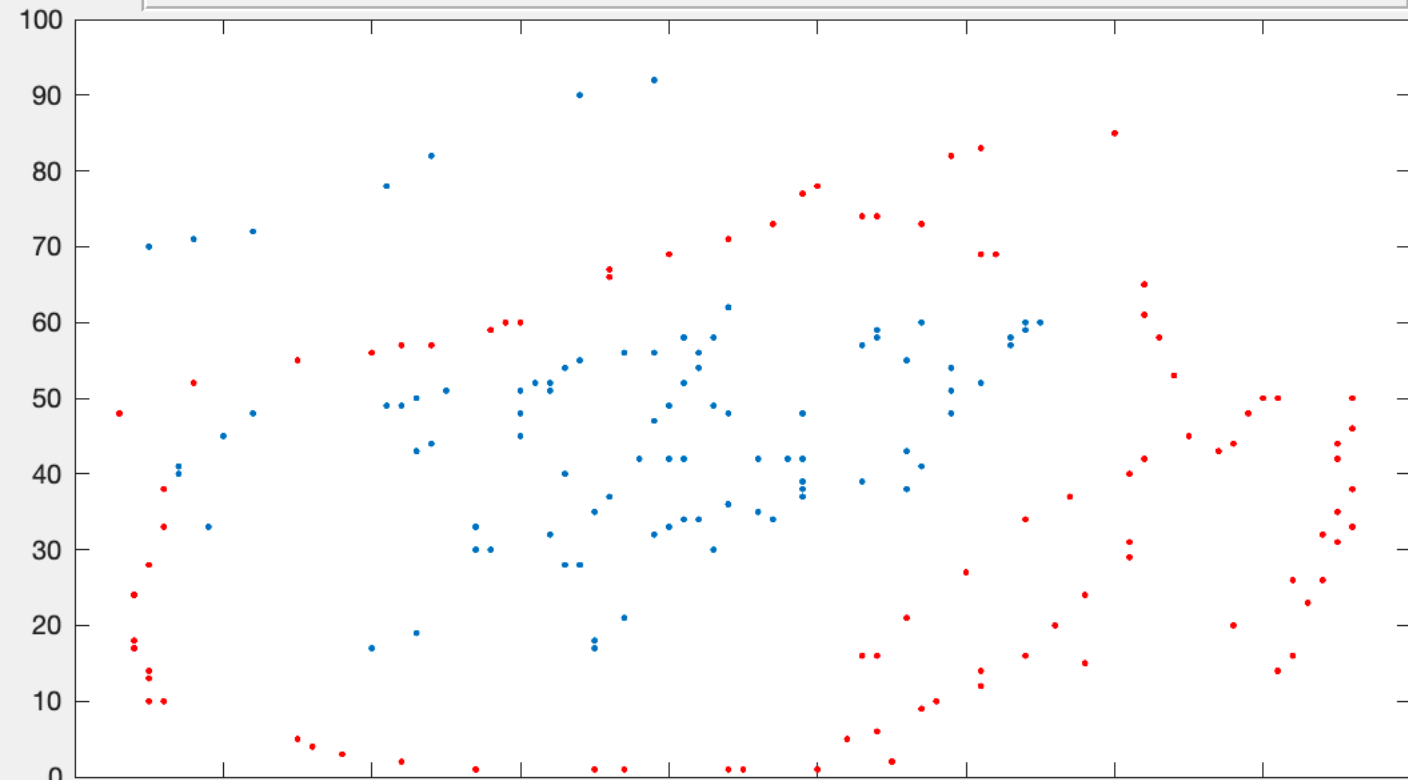
Nonlinear separation for Classification

Numerical Methods
AM NDHU

Fileing

New PenData OK

LOAD SAVE JimData

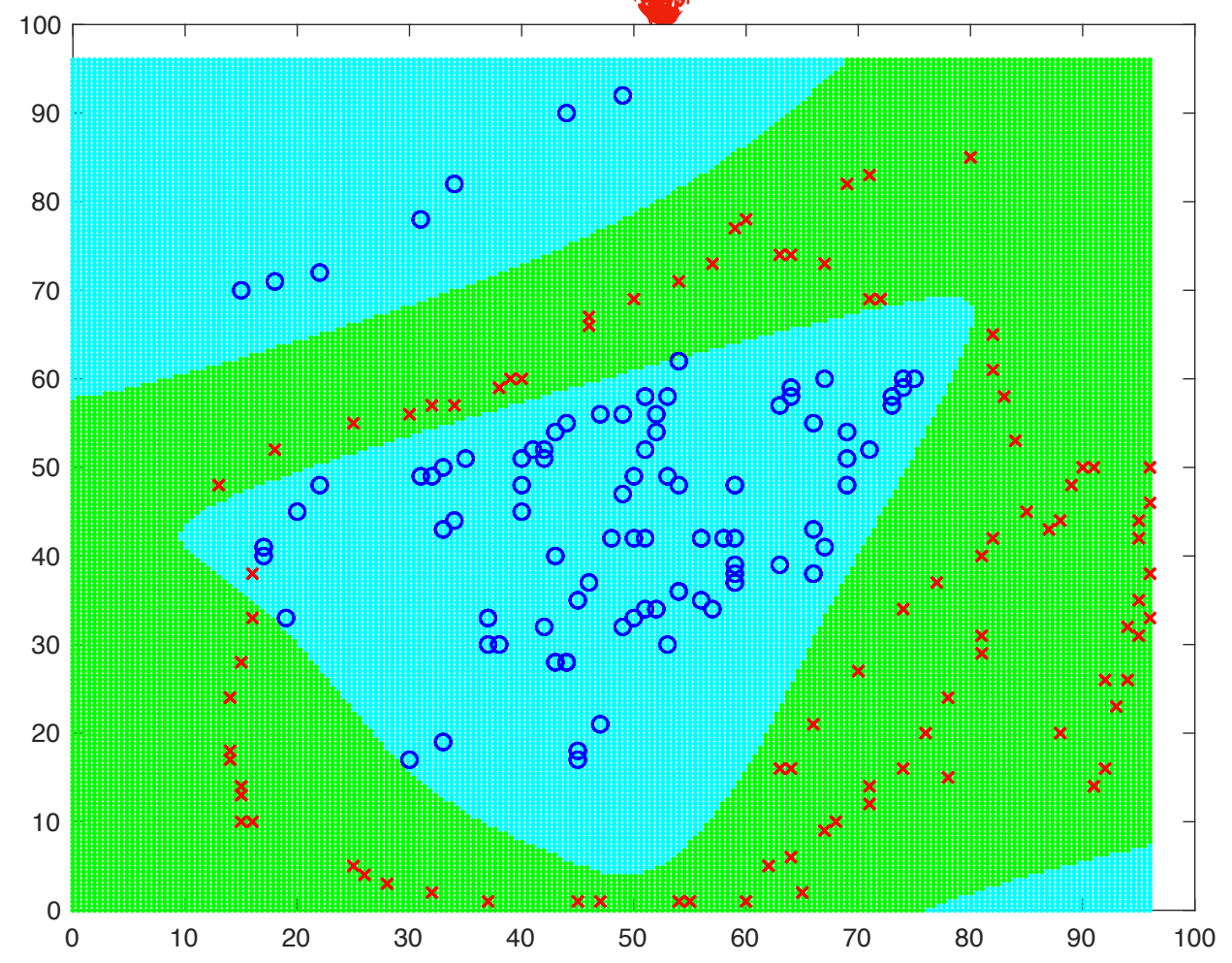
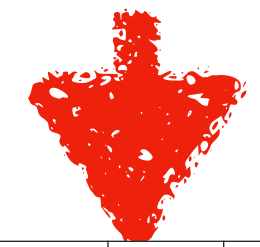


Process

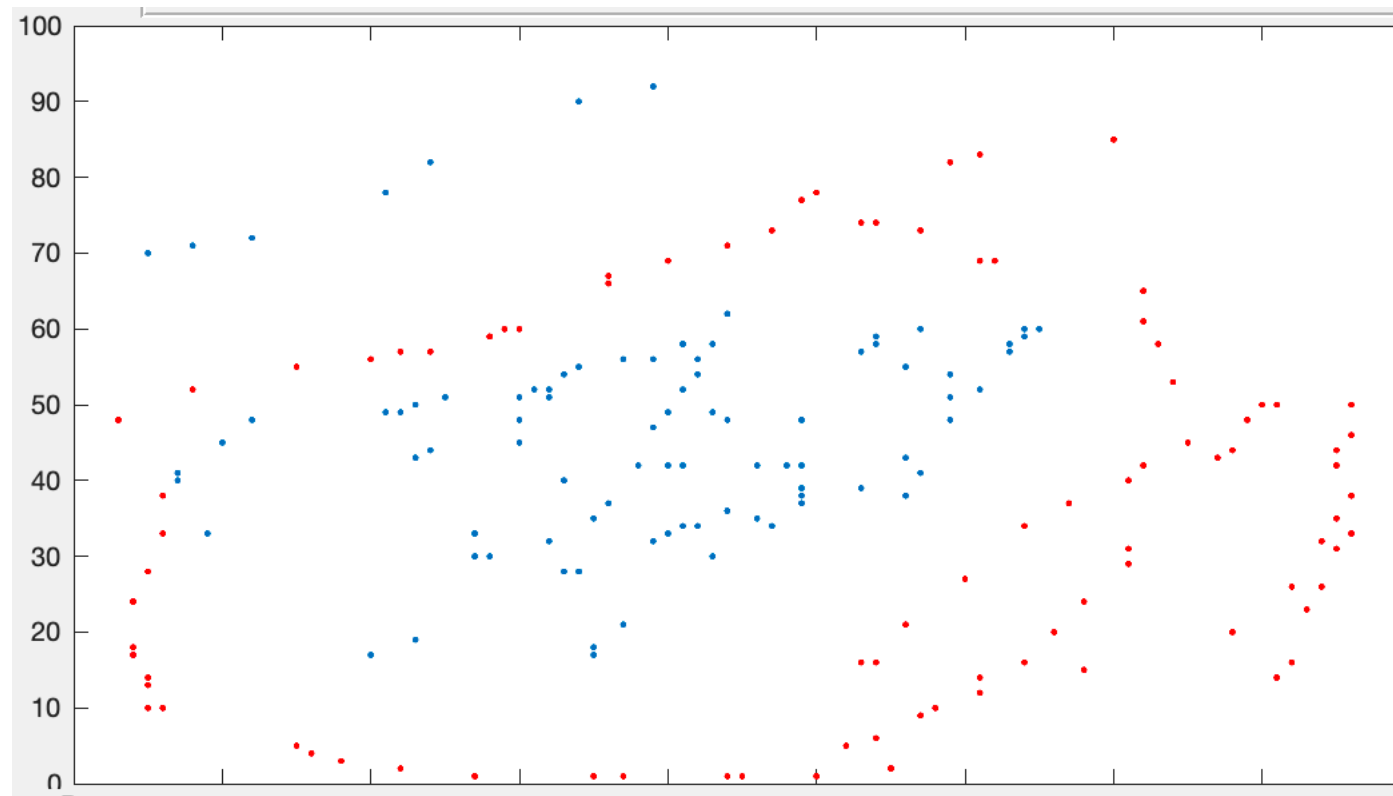
MLPotts learning 10 21

Linear Separation 0.004902 err rate

Supervised Learning
for classification



Each point has a label. Its color is either red or blue.



Predictors or stimuli: $X = \{x[t] \in R^2\}_{t=1}^N$

Responses: $Y = \{y[t] \in \{0,1\}\}_{t=1}^N$

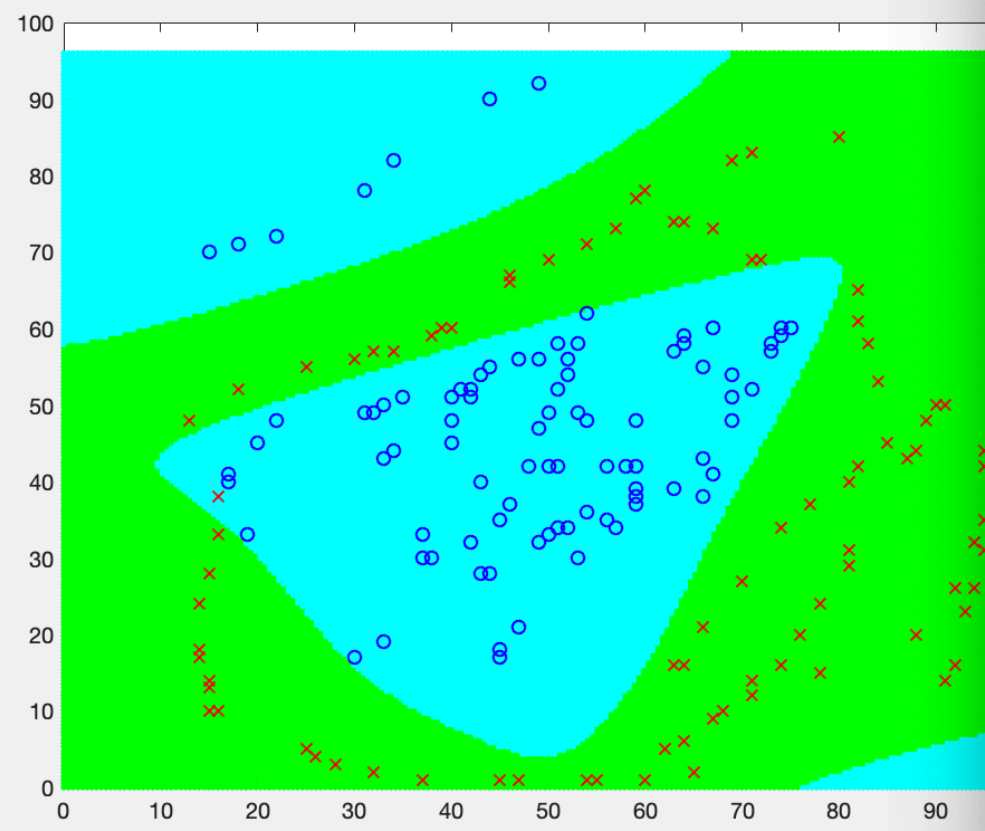
The training data are composed of *labeled patterns*.

$$S = \{(x[t], y[t]) \mid x[t] \in R^2, y[t] \in \{0,1\}\}_{t=1}^N$$

The data space has been well partitioned to two exclusive regions, in each of which training data are with the same label

```
425  
426 % handles empty
```

Figure 3
File Edit View Insert Tools Desktop Window Help



SeparableTest

Nonlinear separation for Classification

Numerical Methods
AM NDHU

New PenData OK

Filing
LOAD SAVE JimData

Process
MLPotts learning 10 21

**What is the learning
error or training error?**

Handwritten digit Classification

$$F(x | \theta_{random})$$



Train a classifier

Training data set:
labeled digits



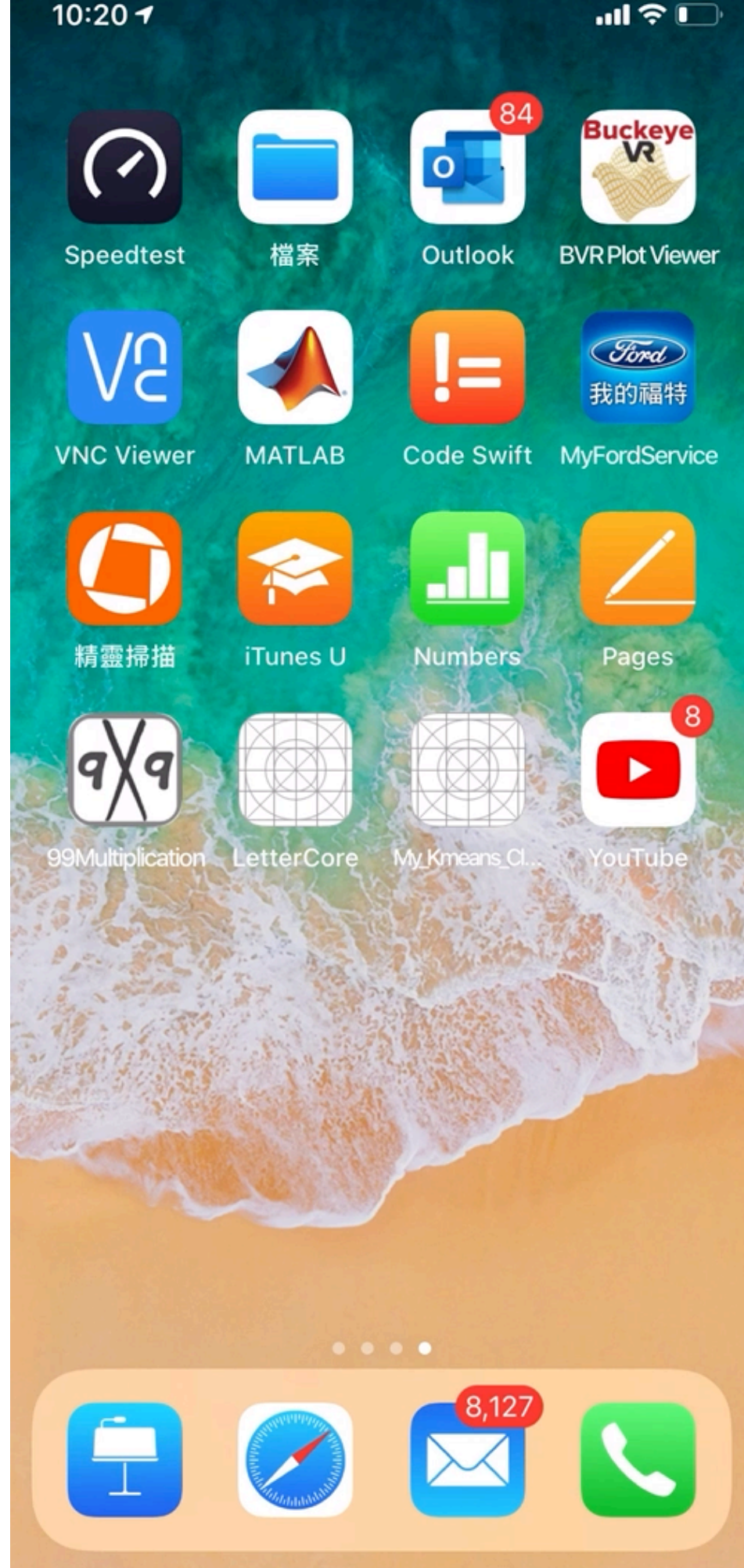
$$F(x | \theta_{opt})$$

Test $F(x | \theta_{opt})$

Testing
data set



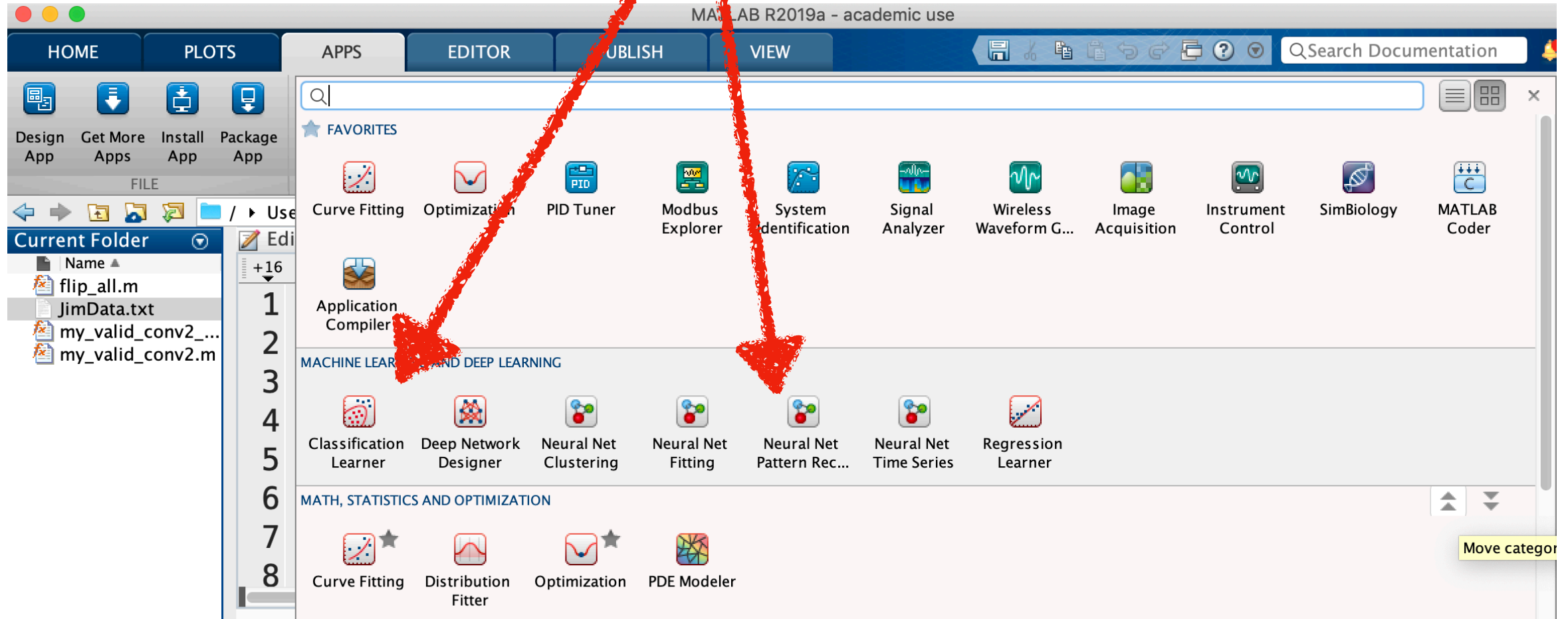
Real application of $F(x | \theta_{opt})$



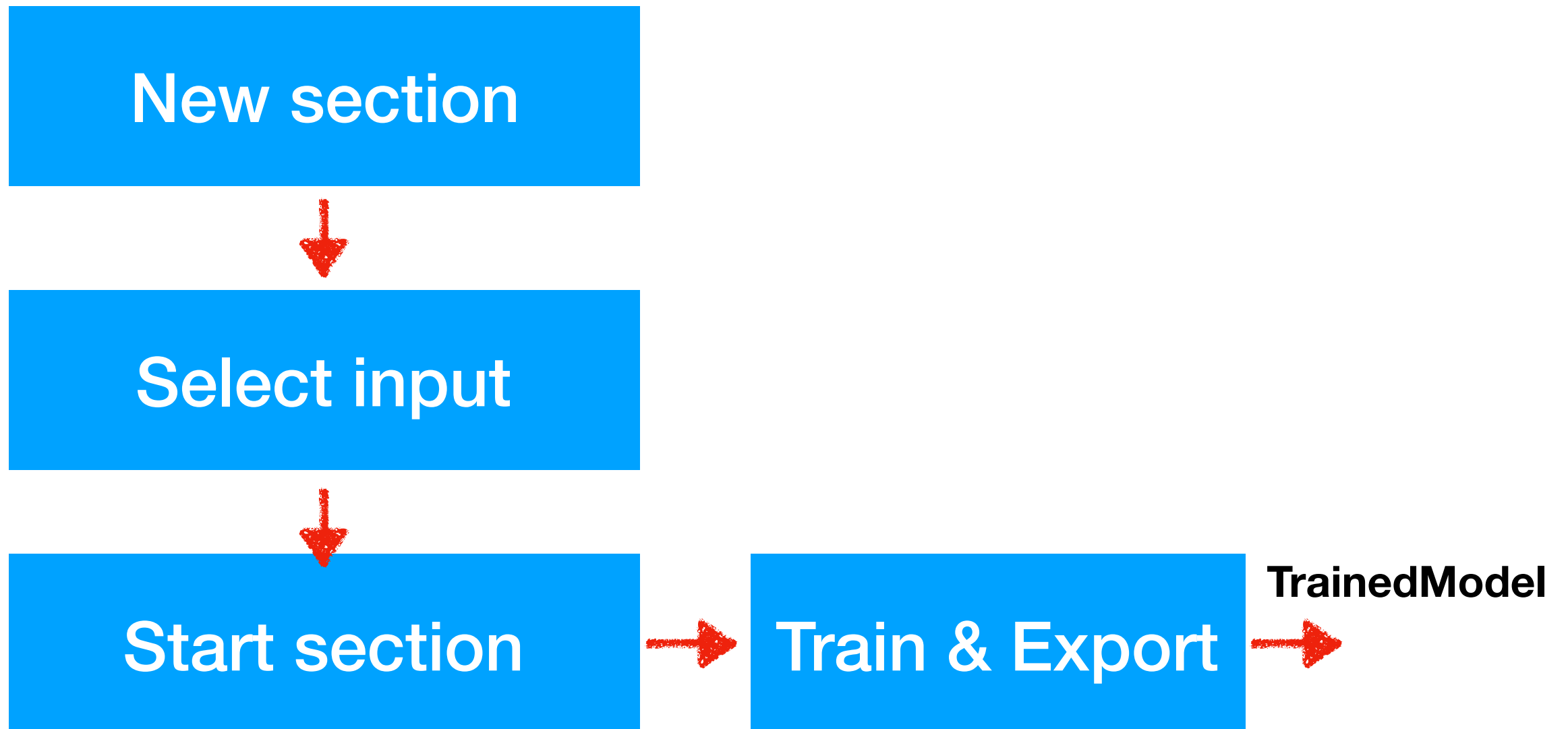
iPhone screen recording

Classifier Learner App

load JimData.txt



Classifier Learner



CLASSIFICATION LEARNER

VIEW



New Session |
 Feature Selection |
 PCA |
 Linear Discrimi... |
 Quadratic Discrimi... |
 All Discrimi... |
 Logistic Regression |
 Advanced |
 Use Parallel |
 Train |
 Scatter Plot |
 Confusion Matrix |
 ROC Curve |
 Parallel Coordinates Plot |
 Export Plot to Figure |
 Generate Function |
 Export Model

FILE FEATURES MODEL TYPE TRAINING PLOTS EXPORT

Data Browser

▼ History

1 ☆ Tree	Accuracy: 100.0%
Last change: Disabled PCA 2/2 features	
2 ☆ Logistic Regression	Accuracy: 65.2%
Last change: Logistic Regression 2/2 features	
3.1 ☆ Naive Bayes	Accuracy: 84.5%
Last change: Gaussian Naive Bayes 2/2 features	
3.2 ☆ Naive Bayes	Accuracy: 86.6%
Last change: Kernel Naive Bayes 2/2 features	
4 ☆ Quadratic Discriminant	Accuracy: 83.8%
Last change: Quadratic Discriminant 2/2 features	

▼ Current Model

Model 4: Trained

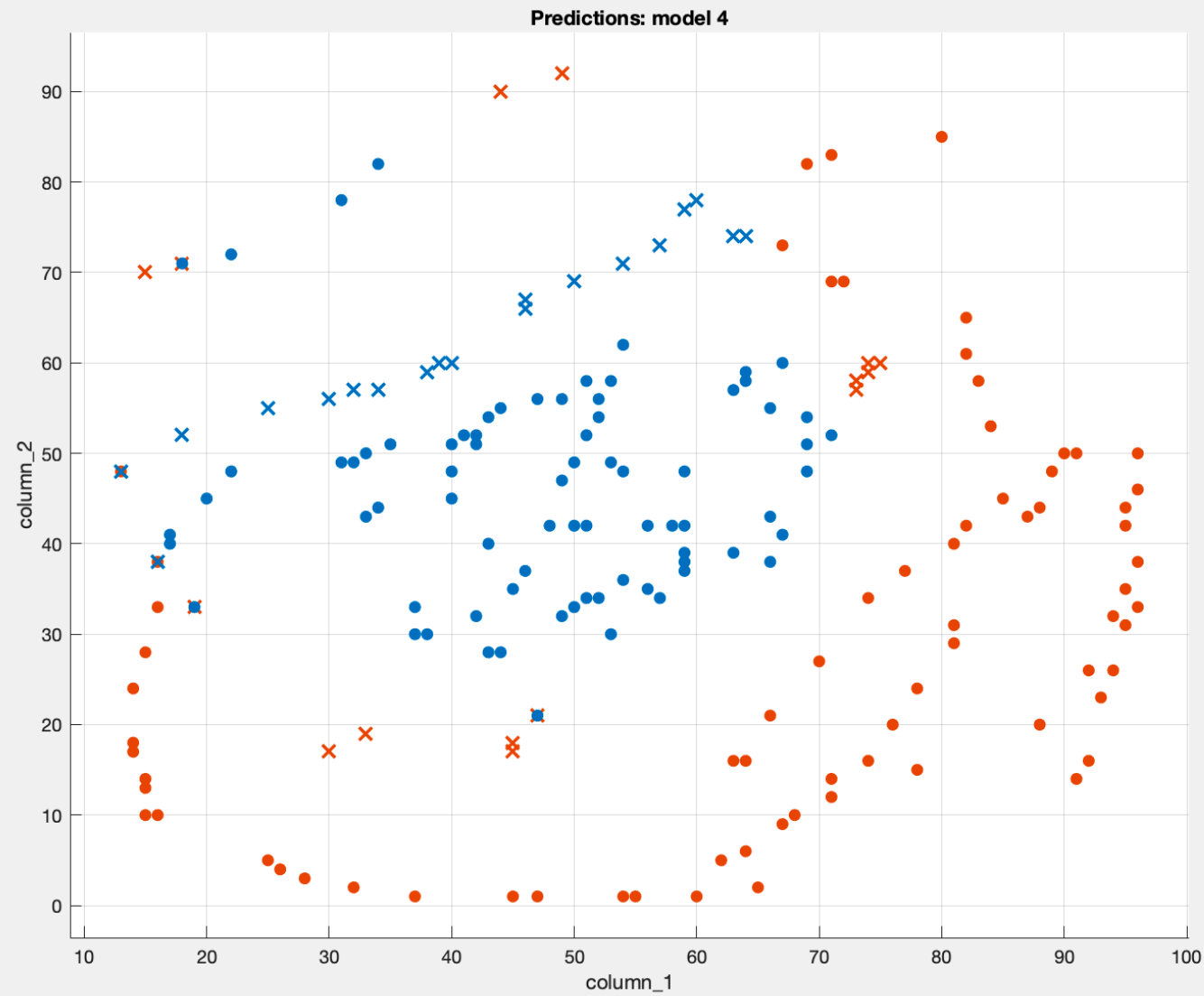
Results

Accuracy	83.8%
Prediction speed	~16000 obs/sec
Training time	4.941 sec

Model Type

Preset: Quadratic Discriminant

Scatter Plot



Plot

Data

Model predictions

- Correct
- Incorrect

Predictors

X: column_1

Y: column_2

Classes Move to Front

Show	Order
<input checked="" type="checkbox"/>	0
<input checked="" type="checkbox"/>	1

[How to investigate features](#)

Exercise III

Select a learner.

**Train a classifier subject to JimData
and export the TrainedModel.**

Exercise IV

Write a Matlab function to evaluate the accuracy of the TrainedModel.

```
function accuracy = my_fit(JimData,trainedModel)
```

```
yfit = trainedModel.predictFcn(X);
```


Exercise V

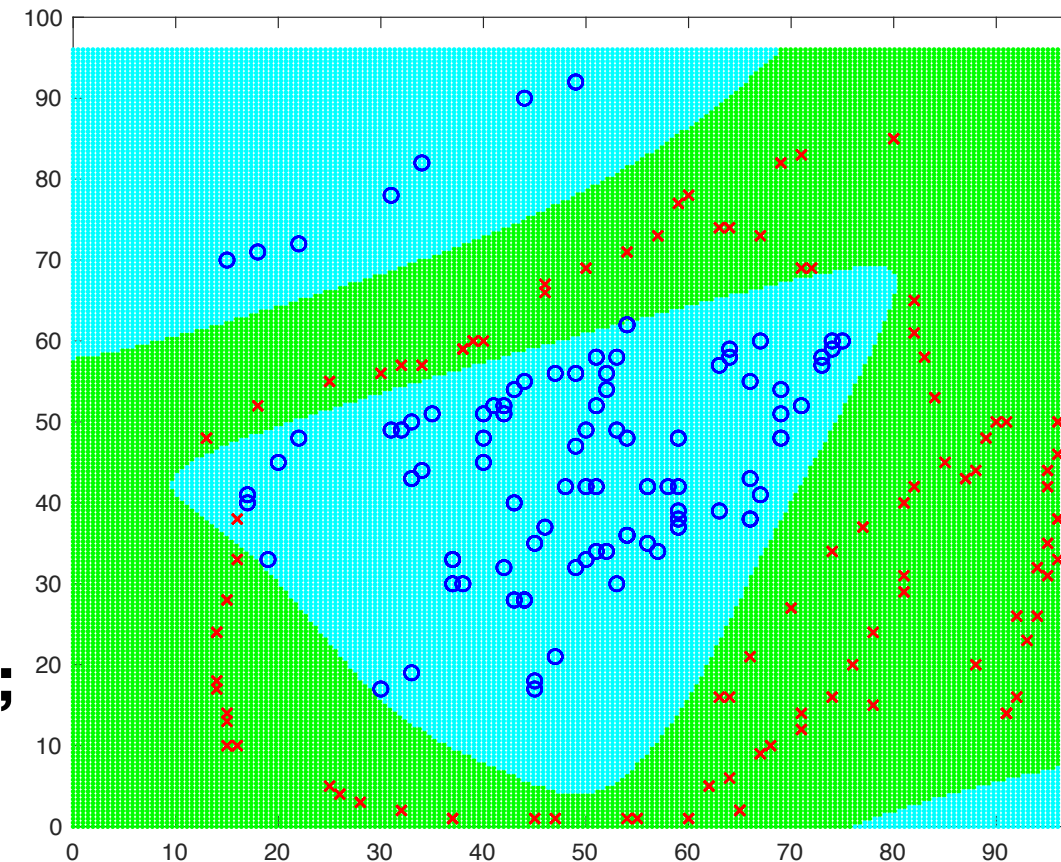
Draw the partitioned exclusive regions of the TRainedModel

```
n=200;  
x1=linspace(0,Net.max_x,n); % revise codes  
x2=x1;  
xx=[repmat(x1',n,1) reshape(repmat(x2,n,1),n*n,1)];  
CC= % write codes  
figure  
ind=find(CC>0.5);  
plot(xx(ind,1),xx(ind,2),'g.');
```

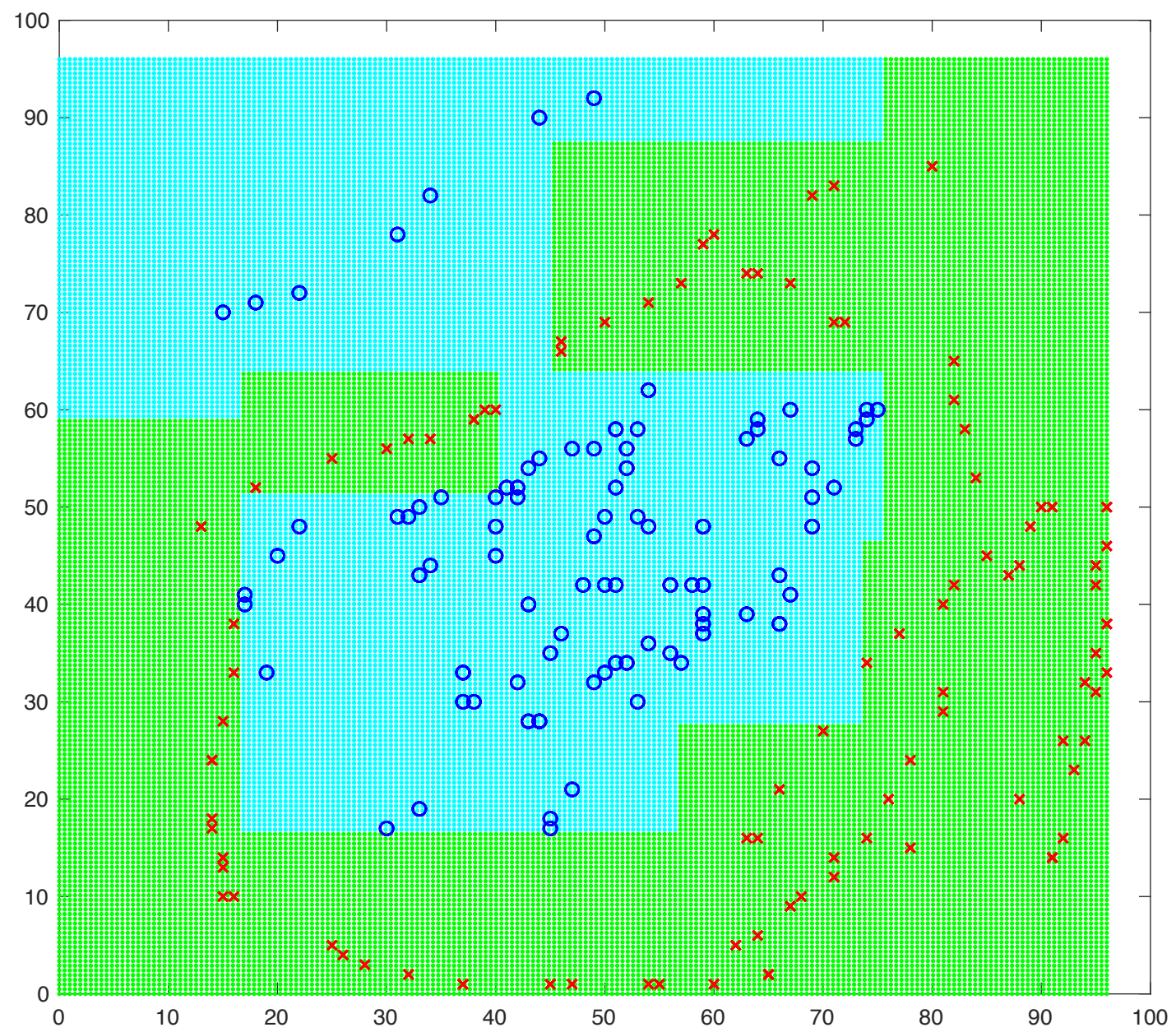
```
hold on  
ind=find(CC<0.5);  
plot(xx(ind,1),xx(ind,2),'c.');
```

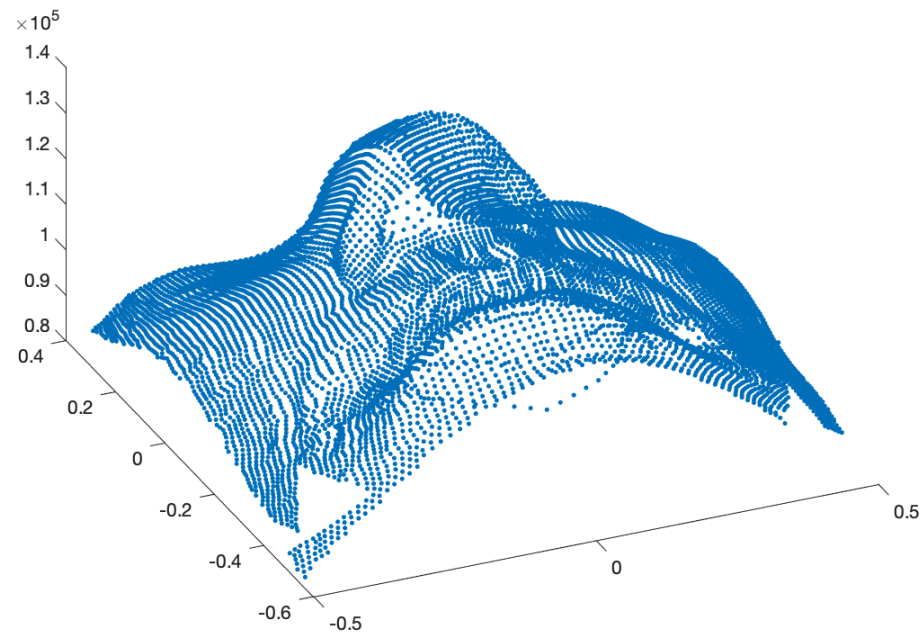
```
pc = JimData(:,3);x_train=JimData(:,1:2)  
plot(x_train(find(pc==0),1),x_train(find(pc==0),2),'oB');
```

```
plot(x_train(find(pc==1),1),x_train(find(pc==1),2),'xR');
```

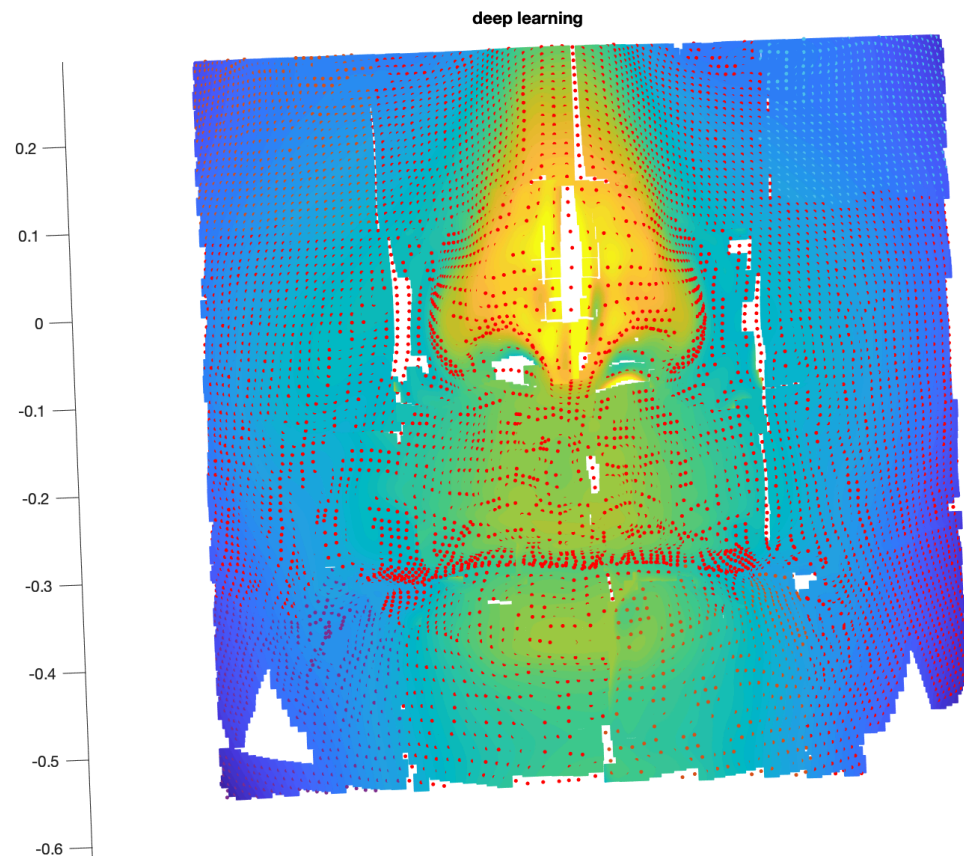



```
n=200;
x1=linspace(0,max(max(X)),n);
x2=x1;
% revise codes
xx=[ repmat(x1',n,1) reshape(repmat(x2,n,1),n*n,1) ];
CC= trainedModel.predictFcn(xx); % write codes
figure
ind=find(CC>0.5);
plot(xx(ind,1),xx(ind,2),'g. '); hold on
ind=find(CC<0.5);
plot(xx(ind,1),xx(ind,2),'c. ');
pc = JimData(:,3);
x_train=JimData(:,1:2);
plot(x_train(find(pc==0),1),x_train(find(pc==0),2),'oB');
plot(x_train(find(pc==1),1),x_train(find(pc==1),2),'xR');
```





圖一、3D人臉的原始資料點



圖九a、完整的臉頰、鼻子、嘴、下巴3D人臉平面幾何重構與近似