

# Voronoi partition

Manhalanobis distance

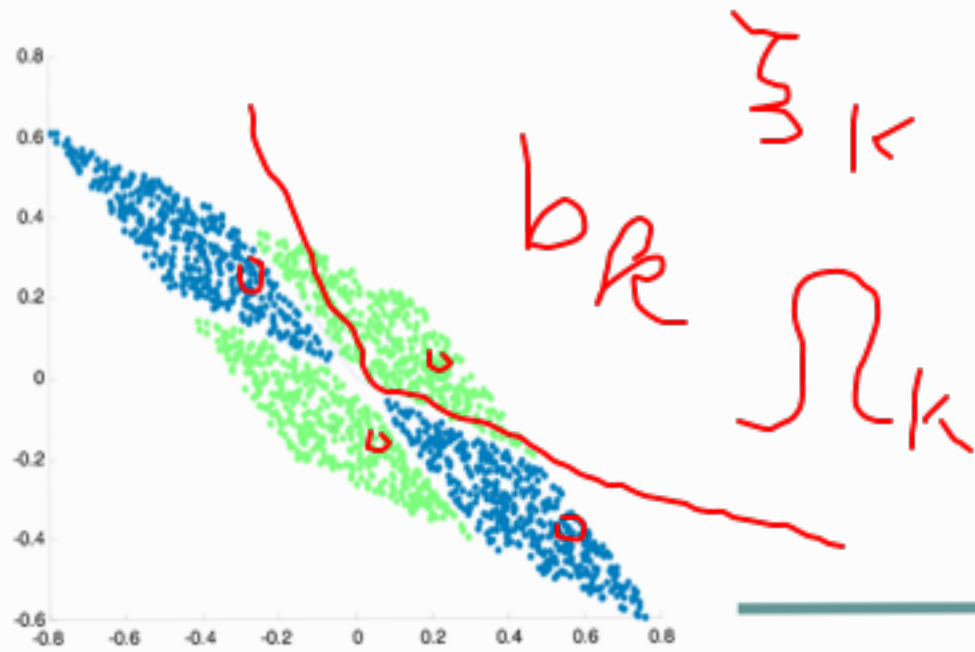
$$\|\mathbf{x} - \mathbf{y}\|_A = \sqrt{(\mathbf{x} - \mathbf{y})^T A (\mathbf{x} - \mathbf{y})}$$

Voronoi Partition defined by A and all  $\mathbf{y}_i$  in  $\theta$

$$\Omega_k = \{x \mid k = \arg \min_j \|\mathbf{x} - \mathbf{y}_j\|_A\}$$

$$\Omega_1 = \{x \mid 1 = \arg \min_k \|x - b_k\|_A\}$$

- Four local means
- Non-overlapping distributions
- A common weight matrix for rotation



$$\theta = \{A, b_1, b_2, b_3, b_4\}$$

$$\sum_k \in \{e_1, e_2\}$$

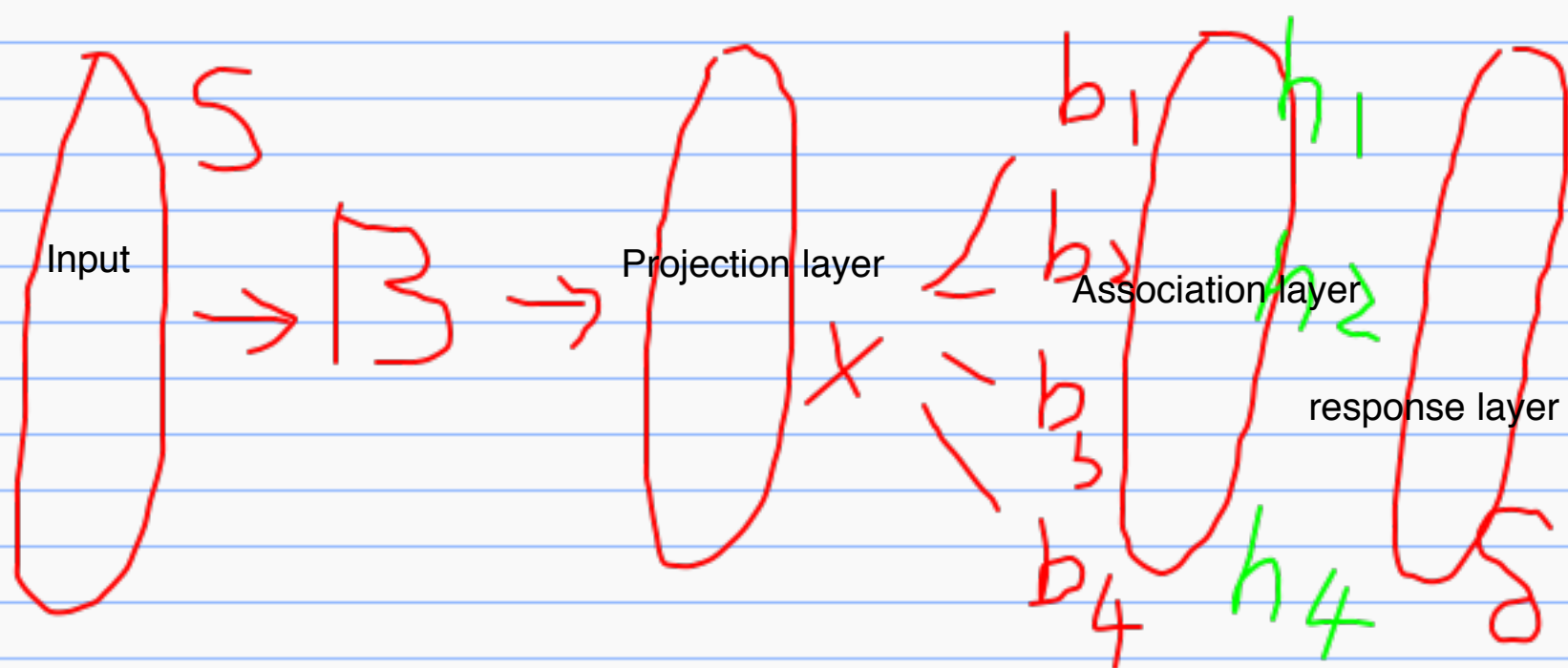
$$k = 1, 2, 3, 4$$

$$\theta = \{A, b_1, b_2, b_3, b_4$$

$$\omega_1, \omega_2, \omega_3, \omega_4\}$$

$$S \rightarrow Bs \rightarrow x$$

a matrix-type  
feature extractor



## Memberships

- Unitary vectors for membership representations

$\mathbf{e}_k$  denotes a unitary vector with the  $k$ th bit one and others zeros

$\Xi_K = \{\mathbf{e}_k\}_{k=1}^K$  denotes collection of possible memberships

$$\delta = \mathbf{e}_k \text{ if } x \in \Omega_k$$

membership of  $x$

$$\|x - b_1\|_A^2 \geq \|x - b_2\|_A^2$$

$$\begin{aligned} x^T A x - 2x^T A b_1 + b_1^T A b_1 &\geq x^T A x - 2x^T A b_2 + b_2^T A b_2 \end{aligned}$$

$$x^T A b_1 \geq x^T A b_2$$

unitary vector assumption.

① let  $B$  be a square matrix

②  $h_k = X^T b_k$

Ex Merib

③  $S = e_k$  if

$k = \underset{j}{\operatorname{arg\,max}} h_j$

$$y = F(S; \theta)$$

$$= \sum_{k=1}^K \xi_k \text{STE}_k$$

Microsoft PowerPoint - lecture-PottsNDA.ppt  
134.208.26.59/NA/lecture-PottsNDA.pdf

### Discriminating function

- $\theta$  and  $\xi$  define a discriminate function

$$\begin{aligned} g(\mathbf{x}_i; \theta, \xi) &= \sum_k \xi_k F(\mathbf{x}_i; \theta) \mathbf{e}_k \\ &= \sum_k \xi_k \delta_i^T \mathbf{e}_k \\ &= \sum_k \sum_m \xi_k \delta_{im} \end{aligned}$$



## Overlapping membership

$$Pr(S = e_{1T}) \propto \exp(\beta h_k)$$

$$V_k = \frac{\exp(\beta h_k)}{\sum_l \exp(\beta h_l)}$$

$\beta \uparrow \rightarrow$  Ex Mem.