- 1. Generating and counting a sequence of ATCG characters
  - (a) (20 pts) Let  $P_a, P_t, P_c$  and  $P_g$  denote probabilities of generating characters 'A', 'T', 'C', and 'G'. It follows

$$P_a + P_t + P_c + P_q = 1.$$

Write a matlab function to generate a sequence of ATCG characters, where occurrence probabilities of the four characters at each position are approximately  $P_a, P_t, P_c$  and  $P_g$ .

- (b) (20 pts) Write a matlab function to count occurrences of the four characters in a string that is generated by the matlab function developed for solving the previous problem.
- 2. (20 pts) Implement the following procedure in a matlab script
  - (a) Get a string that specifies a one-dimensional function, f(x).
  - (b) Plot f(x) for  $x \in [-5, 5]$ .
  - (c) Plot f'(x) for  $x \in [-5, 5]$ .
- 3. (20 pts) Let A and B denote two N-by-N matrices. Use nested FOR loops to determine the product of A and B. The kernel of nested FOR loops mainly executes

$$C(i, j) = A(i, :) * B(:, j),$$

where C denotes the result of multiplication.

4. (20 pts) Write a matlab function to find the minimum of

$$g(x_1, x_2) = (x_1^2 + x_2^2 - 13)^2$$

subject to

$$\begin{array}{rrrr} -2 & \leq & x_1 \leq 10 \\ 0 & \leq & x_2 \leq 10 \\ x_2 & \leq & x_1 \end{array}$$