

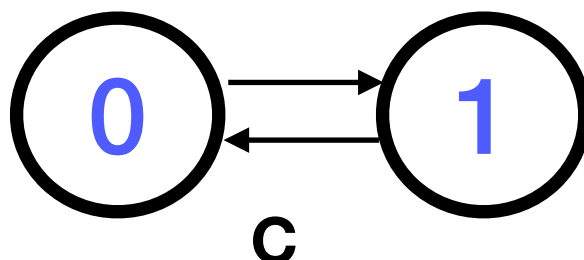
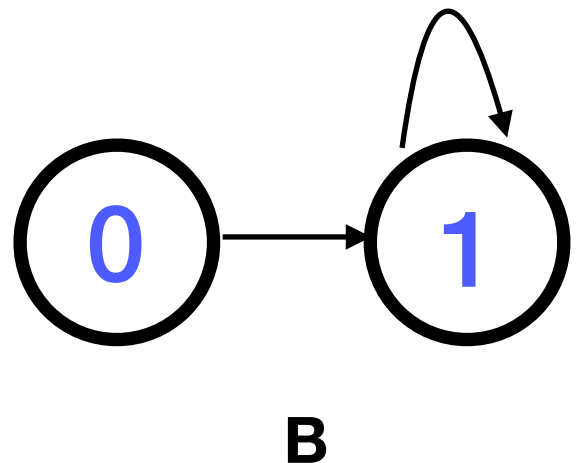
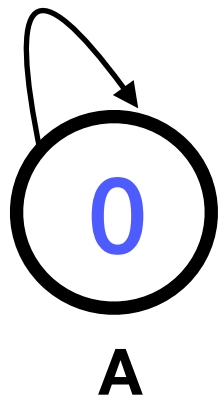
Discrete Math 2018

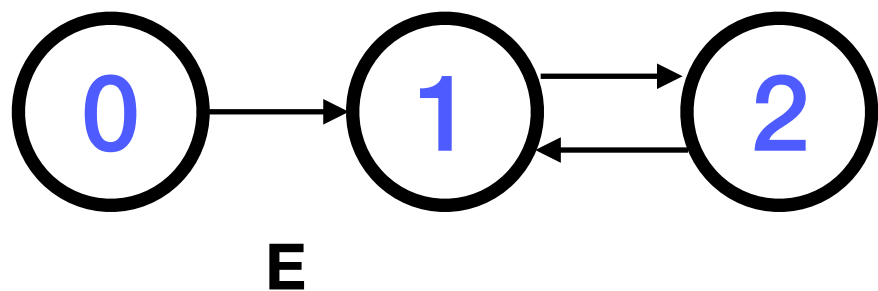
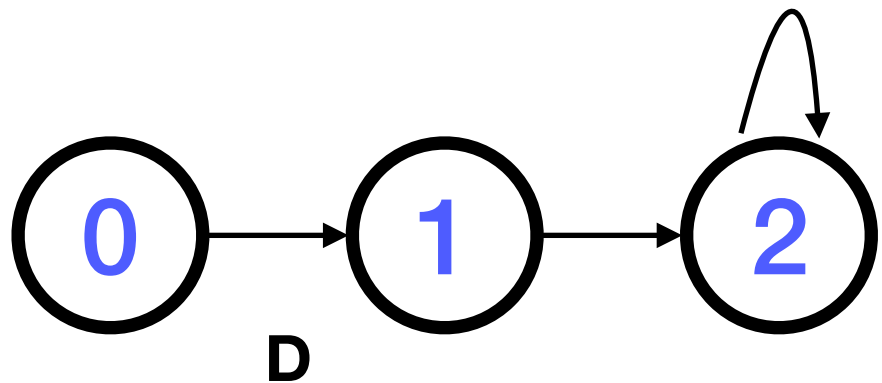
problem set 1

1. Let S denote a single-valued “successor” function. The following axioms define the arithmetical properties of the natural numbers.

- ① For every natural number n , $S(n)$ is a natural number.
- ② For all natural numbers m and n , $m = n$ if and only if $S(m) = S(n)$. That is, S is an **injection**.
- ③ For every natural number n , $S(n) = 0$ is false. That is, there is no natural number whose successor is 0.

A. In the following diagram, $S(m)=n$, if a directed edge connects node m to node n . State why each of the following model is invalid.





B. Try to draw a model that is valid under the three axioms.

2. True tables

A. NOT p

B. p AND q

C. p XOR q

D. p OR q

E. p implies q

F. p if and only if q

3. Show that $\sim(p \oplus q) \equiv p \leftrightarrow q$ using truth table

4. Show that $\sim p \vee q \equiv p \rightarrow q$